

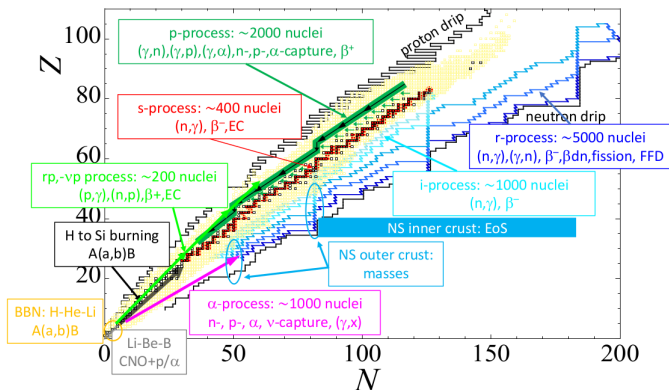
Symmetry breaking on the scale of the nuclear chart

W. Ryssens, G. Scamps, M. Bender, & S. Goriely

29th of September 2021



Where did the elements originate?



M. Arnould & S. Goriely, Prog. Part. Nuc. Phys. **112**, 103766 (2020).

Energy density functionals (EDFs)

$$E \sim \int d^3r \left[C^\rho \rho(\vec{r})\rho(\vec{r}) + C^\tau \rho(\vec{r})\tau(\vec{r}) + \dots \right]$$

- Pheno. form and fit of C 's
- Simple mean-field ansatz

Energy density functionals (EDFs)

$$E \sim \int d^3r \left[C^\rho \rho(\vec{r})\rho(\vec{r}) + C^\tau \rho(\vec{r})\tau(\vec{r}) + \dots \right]$$

- Pheno. form and fit of C 's
- Simple mean-field ansatz
- + microscopic method
- + feasible for 1000s of nuclei

Energy density functionals (EDFs)

$$E \sim \int d^3r \left[C^\rho \rho(\vec{r})\rho(\vec{r}) + C^\tau \rho(\vec{r})\tau(\vec{r}) + \dots \right]$$

- Pheno. form and fit of C 's
- Simple mean-field ansatz
- + microscopic method
- + feasible for 1000s of nuclei

"Structure" fits

- Study observables **locally**
- Fitted on $\lesssim 10$ nuclei
- Typically ~ 15 parameters
- **Advanced** calculations

Energy density functionals (EDFs)

$$E \sim \int d^3r \left[C^{\rho} \rho(\vec{r})\rho(\vec{r}) + C^{\tau} \rho(\vec{r}) \tau(\vec{r}) + \dots \right]$$

- Pheno. form and fit of C 's
- Simple mean-field ansatz
- + microscopic method
- + feasible for 1000s of nuclei

"Structure" fits

- Study observables **locally**
- Fitted on $\lesssim 10$ nuclei
- Typically ~ 15 parameters
- **Advanced** calculations

"Astro" fits

- Study **global** masses
- More parameters (22)
- **Simplified** calculations

Energy density functionals (EDFs)

$$E \sim \int d^3r \left[C^\rho \rho(\vec{r})\rho(\vec{r}) + C^\tau \rho(\vec{r})\tau(\vec{r}) + \dots \right]$$

- Pheno. form and fit of C 's
- Simple mean-field ansatz
- + microscopic method
- + feasible for 1000s of nuclei

"Structure" fits

- Study observables **locally**
- Fitted on $\lesssim 10$ nuclei
- Typically ~ 15 parameters
- **Advanced** calculations

"Astro" fits

- Study **global** masses
- **!** Fitted on **2408** masses
- More parameters (22)
- **Simplified** calculations

Energy density functionals (EDFs)

$$E \sim \int d^3r \left[C^\rho \rho(\vec{r})\rho(\vec{r}) + C^\tau \rho(\vec{r})\tau(\vec{r}) + \dots \right]$$

- Pheno. form and fit of C 's
- Simple mean-field ansatz
- + microscopic method
- + feasible for 1000s of nuclei

"Structure" fits

- Study observables **locally**
 - Fitted on $\lesssim 10$ nuclei
 - Typically ~ 15 parameters
 - **Advanced** calculations
- $\sigma_{\text{rms}}(M) \sim \mathbf{2-10}$ MeV

"Astro" fits

- Study **global** masses
- **!** Fitted on **2408** masses
- More parameters (22)
- **Simplified** calculations

Energy density functionals (EDFs)

$$E \sim \int d^3r \left[C^\rho \rho(\vec{r})\rho(\vec{r}) + C^\tau \rho(\vec{r})\tau(\vec{r}) + \dots \right]$$

- Pheno. form and fit of C 's
- Simple mean-field ansatz
- + microscopic method
- + feasible for 1000s of nuclei

"Structure" fits

- Study observables **locally**
 - Fitted on $\lesssim 10$ nuclei
 - Typically ~ 15 parameters
 - **Advanced** calculations
- $\sigma_{\text{rms}}(M) \sim \mathbf{2-10}$ MeV

"Astro" fits

- Study **global** masses
 - **!** Fitted on **2408** masses
 - More parameters (22)
 - **Simplified** calculations
- $\sigma_{\text{rms}}(M) \sim \mathbf{0.6}$ MeV

Energy density functionals (EDFs)

$$E \sim \int d^3r \left[C^{\rho} \rho(\vec{r})\rho(\vec{r}) + C^{\tau} \rho(\vec{r})\tau(\vec{r}) + \dots \right]$$

- Pheno. form and fit of C 's
- Simple mean-field ansatz
- + microscopic method
- + feasible for 1000s of nuclei

"Structure" fits

- Study observables **locally**
 - Fitted on $\lesssim 10$ nuclei
 - Typically ~ 15 parameters
 - **Advanced** calculations
- $\sigma_{\text{rms}}(M) \sim \mathbf{2-10}$ MeV

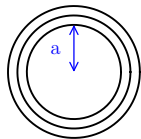
"Astro" fits

- Study **global** masses
 - **!** Fitted on **2408** masses
 - More parameters (22)
 - **Simplified** calculations
- $\sigma_{\text{rms}}(M) \sim \mathbf{0.6}$ MeV

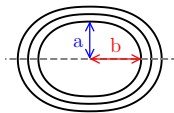
We are bringing the "structure" to the "astro" scale!

Symmetry breaking and nuclear shapes

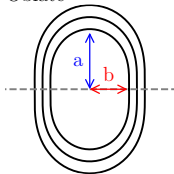
Spherical



Prolate



Oblate



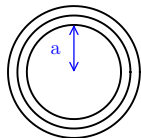
One DOF: β_{20}

State-of-the-art "Astro" fits

- Axial symmetry

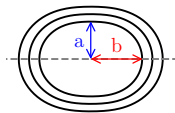
Symmetry breaking and nuclear shapes

Spherical

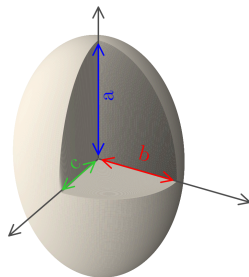
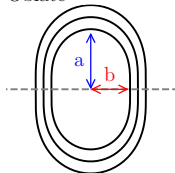


One DOF: β_{20}

Prolate



Oblate



Two DOF: (β_{20}, β_{22}) or (β, γ)

State-of-the-art "Astro" fits

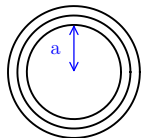
- Axial symmetry

"Structure" calculations

- Triaxial deformation

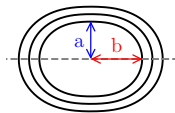
Symmetry breaking and nuclear shapes

Spherical

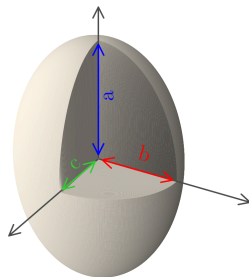
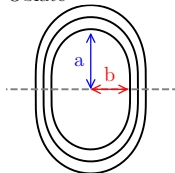


One DOF: β_{20}

Prolate



Oblate



Two DOF: (β_{20}, β_{22}) or (β, γ)

State-of-the-art "Astro" fits

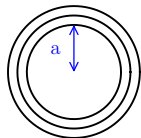
- Axial symmetry

"Structure" calculations

- Triaxial deformation

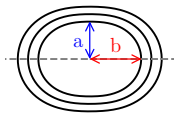
Symmetry breaking and nuclear shapes

Spherical

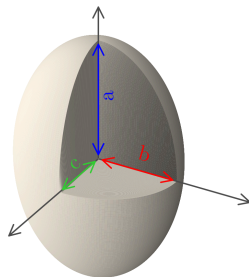
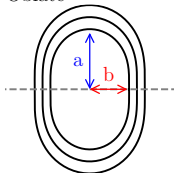


One DOF: β_{20}

Prolate



Oblate



Two DOF: (β_{20}, β_{22}) or (β, γ)

State-of-the-art "Astro" fits

- Axial symmetry
- Time-reversal symmetry
- Reflection symmetry

"Structure" calculations

- **Triaxial deformation**
- Time-reversal breaking
- Octupole deformation

Ingredients

- Standard Skyrme functional
- rotational correction
- 22 parameters

Techniques

BskG = Brussels Skyrme on a Grid

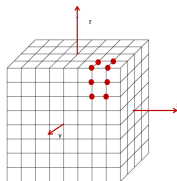
Ingredients

- Standard Skyrme functional
- rotational correction
- 22 parameters

Techniques

- MOCCa
- + 3D coordinate grid
- + Fast and numerically accurate

```
);  
) ; ( (   
( ( ) ;  
, - " " " - .  
, - | ' - . . - ' |  
(( _ | |  
' - \ |  
' . _ _ _ ' ,
```



BskG = Brussels Skyrme on a Grid

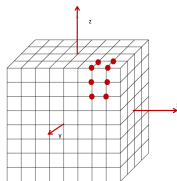
Ingredients

- Standard Skyrme functional
- rotational correction
- 22 parameters
- Fitted to **2408** masses
- and **884** charge radii

Techniques

- MOCCa
- + 3D coordinate grid
- + Fast and numerically accurate

```
      ; ,  
      ) ; ( (   
      ( ( ) ;  
      , - " " " - .  
      , - | ' - . . - ' |  
      (( _ |           |  
      ' - \           /  
      ' . _ _ _ ' ,
```



BSkG = Brussels Skyrme on a Grid

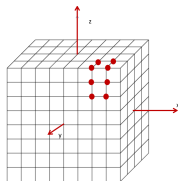
Ingredients

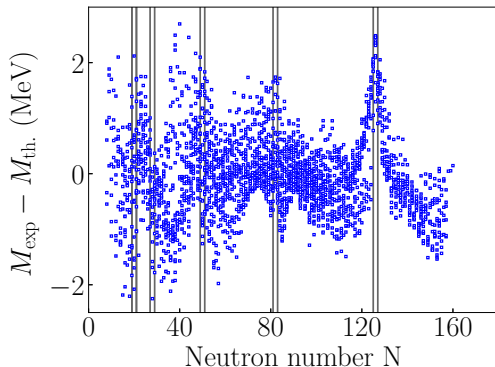
- Standard Skyrme functional
- rotational correction
- 22 parameters
- Fitted to **2408** masses
- and **884** charge radii

Techniques

- MOCCa
- + 3D coordinate grid
- + Fast and numerically accurate
- Machine learning

```
 ; ,  
 ) ; ( (   
 ( ( ) ;  
 , - " " " - ,  
 , - | ' - . . - ' |  
 (( _ | |  
 ' - \ | /  
 ' . _ _ _ ' ,
```



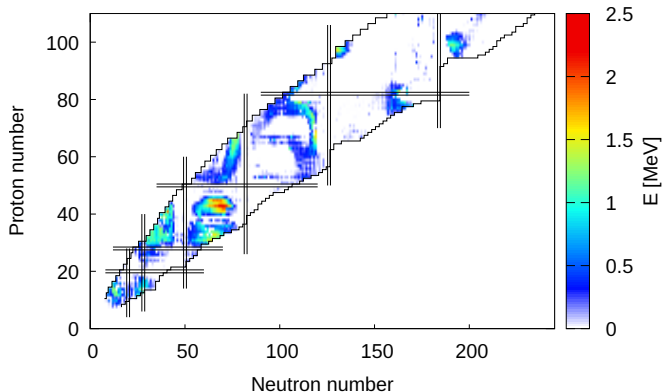


	BSkG1	HFB-21	FRDM (2012)
$\sigma(M)$ (MeV)	0.741	0.577	0.560
$\sigma(R_c)$ (fm)	0.024	0.027	0.038

HFB-21: S. Goriely *et al.*, PRC **82**, 035804 (2010).

FRDM: P. Möller *et al.*, At. Data Nucl. Data Tables, **109-110** (2016).

Triaxiality: where?

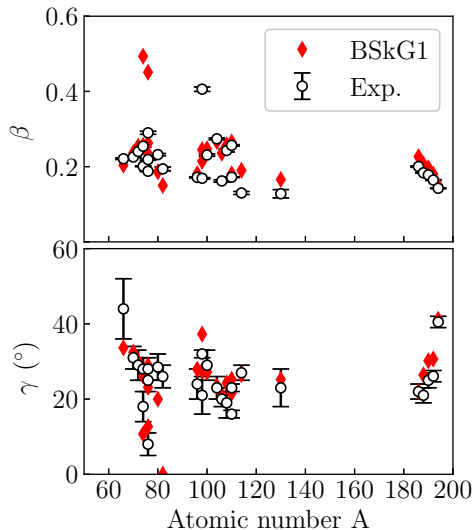


	BSkG1	HFB-21	FRDM (2012)
$\sigma(M)$ (MeV)	0.741	0.577	0.560
$\sigma(R_C)$ (fm)	0.024	0.027	0.038

HFB-21: S. Goriely *et al.*, PRC **82**, 035804 (2010).

FRDM: P. Möller *et al.*, At. Data Nucl. Data Tables, **109-110** (2016).

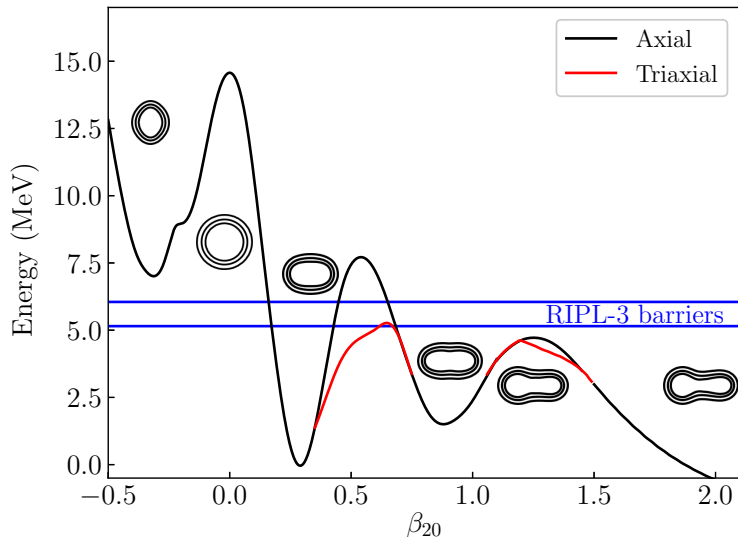
Triaxiality: comparison to experiment

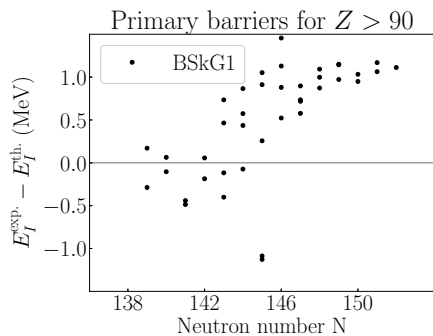


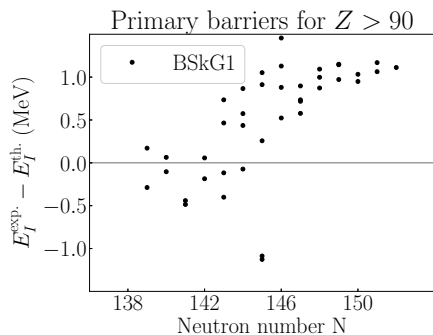
Exp. data from COULEX extracted by M. Zielińska

- M. Rocchini et al., PRC **103**, 014311 (2021).
M. Sugawara et al., EPJA, **16**, 409 (2003).
A. D. Ayangeakaa et al., PLB **754**, 254 (2016).
Y. Toh et al., EPJA **9**, 353 (2000).
A. D. Ayangeaka et al., PRL **123**, 102501 (2019).
E. Clément et al., PRC **75**, 054313 (2007).
A. E. Kavka et al., NPA **593**, 177 (1995).
E. Clément et al., PRC **94**, 054326 (2016).
M. Zielińska, Ph.D. thesis, Warsaw U., 2005.
M. Zielińska et al., NPA **712**, 3 (2002).
K. Wrzosek-Lipska et al., PRC **86**, 064305 (2012).
J. Srebrny et al., NPA **766**, 25 (2006).
K. Wrzosek-Lipska et al., APB **51**, 789 (2020).
C. Fahlander et al., NPA **485**, 327 (1988).
L. E. Svensson et al., NPA **584**, 547 (1995).
L. Morrison et al., PRC **102**, 054304 (2020).
C. Y. Wu et al., NPA **607**, 178 (1996).

^{240}Pu with BSkG1

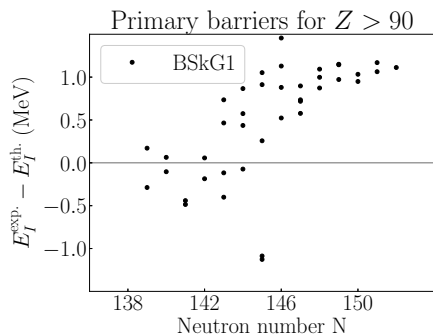






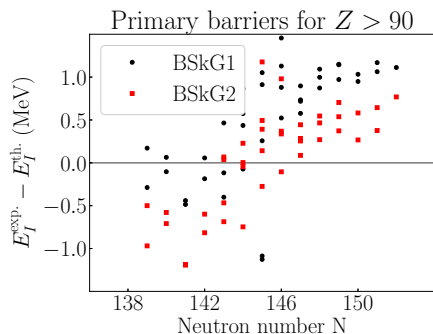
BSkG2

- Fit with complete \tilde{T} -breaking
- 22 + **3** parameters
- Vibrational correction



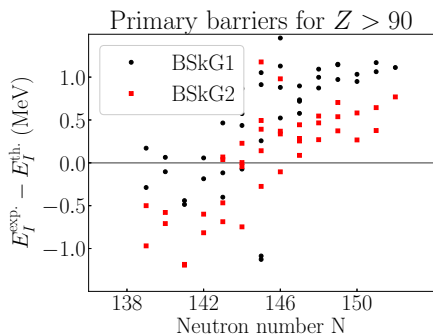
BSkG2

- Fit with complete \tilde{T} -breaking
- 22 + **3** parameters
- Vibrational correction
- fit to RIPL-3 data for **12** even-even nuclei
- Full eval.: 40 barriers $Z \geq 90$



BSkG2

- Fit with complete \tilde{T} -breaking
- 22 + **3** parameters
- Vibrational correction
- fit to RIPL-3 data for **12** even-even nuclei
- Full eval.: 40 barriers $Z \geq 90$



BSkG2

- Fit with complete \tilde{T} -breaking
- 22 + **3** parameters
- Vibrational correction
- fit to RIPL-3 data for **12** even-even nuclei
- Full eval.: 40 barriers $Z \geq 90$

	BSkG1	BSkG2	HFB-14	FR(L)DM
$\sigma(M)$ (MeV)	0.741	0.668	0.729	0.560
$\sigma(E_I)$ (MeV)	0.853	0.447	0.621	0.767

HFB-14 from S. Goriely *et al.*, PRC **75**, 064312 (2007).

FRDM from P. Möller *et al.*, At. Data Nucl. Data Tables, **109-110** (2016).

BSkG1

- Large-scale mass model
- fitted to **2408** masses
- on a 3D mesh, ML fit
- ground state triaxiality

Conclusions & Outlook

BSkG1

- Large-scale mass model
- fitted to **2408** masses
- on a 3D mesh, ML fit
- ground state triaxiality

G. Scamps *et al.*,
arXiv:2011.07904 (nucl-th)

Conclusions & Outlook

BSkG1

- Large-scale mass model
- fitted to **2408** masses
- on a 3D mesh, ML fit
- ground state triaxiality

BSkG2

- The next generation
- Full \tilde{T} -breaking
- Added vibrational corr.
- Improved fission barriers

G. Scamps *et al.*,
arXiv:2011.07904 (nucl-th)

Conclusions & Outlook

BSkG1

- Large-scale mass model
- fitted to **2408** masses
- on a 3D mesh, ML fit
- ground state triaxiality

G. Scamps *et al.*,
arXiv:2011.07904 (nucl-th)

BSkG2

- The next generation
- Full \check{T} -breaking
- Added vibrational corr.
- Improved fission barriers

W.R. *et al.*,
in preparation.

Conclusions & Outlook

BSkG1

- Large-scale mass model
- fitted to **2408** masses
- on a 3D mesh, ML fit
- ground state triaxiality

G. Scamps *et al.*,
arXiv:2011.07904 (nucl-th)

BSkG2

- The next generation
- Full \tilde{T} -breaking
- Added vibrational corr.
- Improved fission barriers

W.R. *et al.*,
in preparation.

Outlook

- (Local) comparisons with experiment underway
- Complete fission model (2000 nuclei, half-lives, ...)
- Fission barriers for odd nuclei
- ...

Conclusions & Outlook

BSkG1

- Large-scale mass model
- fitted to **2408** masses
- on a 3D mesh, ML fit
- ground state triaxiality

G. Scamps *et al.*,
arXiv:2011.07904 (nucl-th)

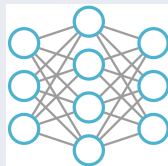
BSkG2

- The next generation
- Full \tilde{T} -breaking
- Added vibrational corr.
- Improved fission barriers

W.R. *et al.*,
in preparation.

Outlook

- (Local) comparisons with experiment underway
- Complete fission model (2000 nuclei, half-lives, ...)
- Fission barriers for odd nuclei
- ...



Thanks!

Thanks for...

... the **help**:

BskG1/2

- S. Goriely ULB
- G. Scamps ULB
- E. Olsen ULB
- J.-F. Lemaître CEA

MOCCa

- P.-H. Heenen ULB
- M. Bender IP2I
- B. Bally UAM

Thanks!

Thanks for...

... the **help**:

BSkG1/2

- S. Goriely ULB
- G. Scamps ULB
- E. Olsen ULB
- J.-F. Lemaître CEA

MOCCa

- P.-H. Heenen ULB
- M. Bender IP2I
- B. Bally UAM

... the **CPU time**:

- CÉCI network, Belgium
- The Zenobe cluster

Thanks!

Thanks for...

... the **help**:

BskG1/2

- S. Goriely ULB
- G. Scamps ULB
- E. Olsen ULB
- J.-F. Lemaître CEA

MOCCa

- P.-H. Heenen ULB
- M. Bender IP2I
- B. Bally UAM

... the **CPU time**:

- CÉCI network, Belgium
- The Zenobe cluster

... the **support**:



Thanks!

Thanks for...

... the **help**:

BSkG1/2

- S. Goriely ULB
- G. Scamps ULB
- E. Olsen ULB
- J.-F. Lemaître CEA

MOCCa

- P.-H. Heenen ULB
- M. Bender IP2I
- B. Bally UAM

... the **CPU time**:

- CÉCI network, Belgium
- The Zenobe cluster

... the **support**:



... your **attention**!