

26 SEP > 1 OCT 2021 Autrans-Méaudre en Vercors, FRANCE

XXIInd COLLOQUE GANIL

Femtoscopic probes of jet-fragmentation mechanisms in INDRA and FAZIA campaigns at GANIL

Q. FABLE

Laboratoire des 2 Infinis de Toulouse - L2IT

INDRA-FAZIA collaboration



- **Context and motivations**
 - The Equation of State of nuclear matter
 - Heavy Ion Collisions at intermediate energies
- **INDRA-VAMOS : HIC peripheral collisions**
 - Isospin transport
 - Experimental setup
 - Observation of isospin transport
- **Nuclear jets fragmentation**
 - Ar+Ni INDRA data highlights
 - Comparisons with models (BLOB)
 - IMF-IMF correlation functions
- **Conclusion and outlooks**



The Equation of State of a nuclear system

$$\delta = (\rho_n - \rho_p) / \rho$$

- The EOS of a nuclear system is defined by its energy per nucleon : $\epsilon(\rho, T, \delta)$
- The density dependence of the symmetry energy term $\epsilon_{sym}(\rho, T)$ remains a major issue in modern nuclear physics :
 - describes the energetic cost of converting isospin symmetric matter into neutron matter ;
 - constraints well established for $T=0K$ and $\rho=\rho_0$ by fitting with nuclear masses ;
 - largely unknown as soon as we move away from normal density.

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Density dependance of ϵ_{sym}

- Taylor expansion :

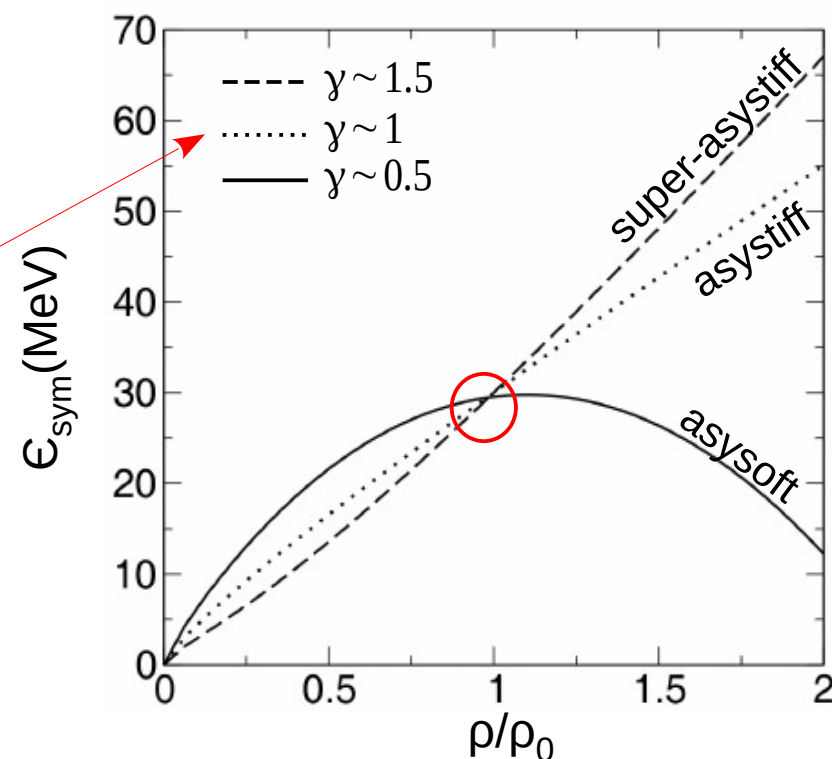
$$\epsilon(\rho, \delta) = \epsilon(\rho, \delta=0) + \epsilon_{sym}(\rho) \cdot \delta^2 + \dots$$

- Ex. of parametrization :

$$\epsilon_{sym}(\rho) = \frac{C_{kin}}{2} \left(\frac{\rho}{\rho_0} \right)^{2/3} + \frac{C_{pot}}{2} \left(\frac{\rho}{\rho_0} \right)^\gamma$$

Kinetic term (Fermi gaz)
Nucleon-nucleon effective interaction term

EOS « stiffness »



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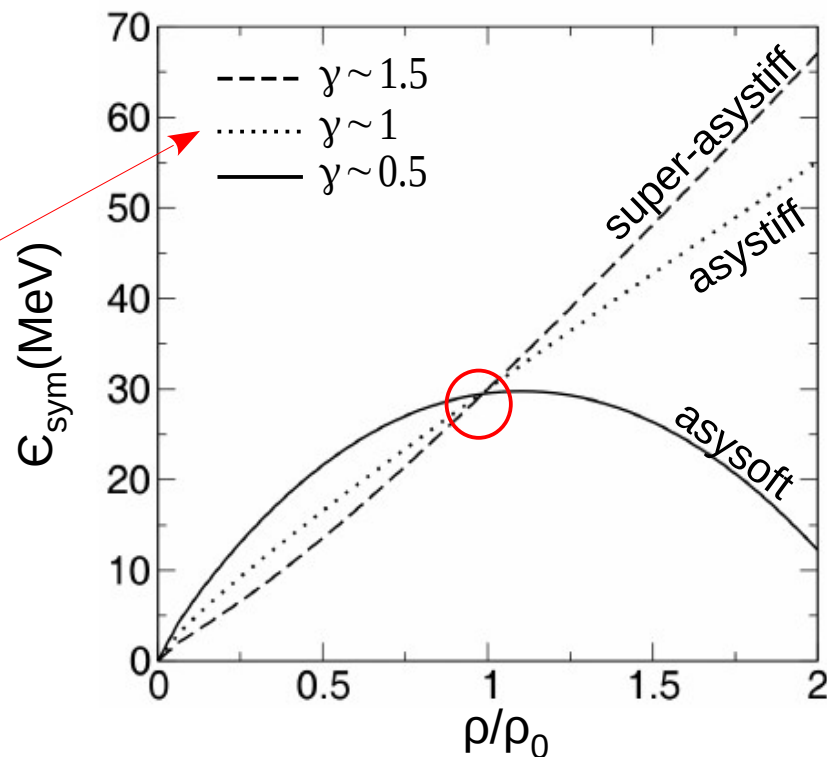
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Kinetic term (Fermi gaz)
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- $\epsilon_{sym}(\rho)$ largely unknown as soon as we move from ρ_0
- Essential information for understanding :
 - Structure of exotic nuclei and neutron skin ;
 - Giant Dipole Resonances and Pygmy Dipole Resonances ;
 - **The dynamic of Heavy Ion Collisions**
- ... but also stellar matter :
 - Supernova explosions mechanisms ;
 - Cooling and composition of neutron stars.



[1] Bao-An Li et al., Phys. Rep. 464

[2] M. Colonna et al., EPJA50:30

[3] G. Martinez-Pinedo et al.,
Jour. Phys. G 41:044008

[4] T. Fischer EPJA50:46

[5] Ad. R. Raduta et. al, EPJA50:24



Heavy Ion Collisions

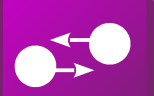
- Formation of exotic nuclei over a wide range of n/p asymmetry
- A tool to study transient states of nuclear matter over various ρ , P , T and J
- Relatively high E^*/A can be reached

Intermediate energies

- $15 \text{ AMeV} \leq E_{inc} \leq 100 \text{ AMeV}$
- Dissipative collisions
- Investigation of $\epsilon_{sym}(\rho)$ in the sub-saturation density regime
→ Domain expected from model calculations

Transport models

- Simulation of the whole dynamic evolution of the colliding system :
 - time evolution of the distributions of the nucleons ;
 - consideration of their quantum features.
- Allow to link experimental observables to the density dependance of the symmetry energy
 - requires extensive comparison of a large variety of observables ;
 - isospin sensitive quantities : isospin transport, isobaric cluster ratios (t/3He), etc...
 - single particle and multi-particle distributions and correlations.
- Symmetry energy is introduced as :
 - Direct input (Mean-field description)
 - Indirect consequence of specific nucleon-nucleon interaction



Heavy Ion Collisions

- Formation of exotic nuclei over a wide range of n/p asymmetry
- Terrestrial way to study transient states of nuclear matter over various ρ , P , T and J
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Transport model (ImQMD05)
 $^{124}\text{Sn} + ^{124}\text{Sn}$ @ 50 A MeV

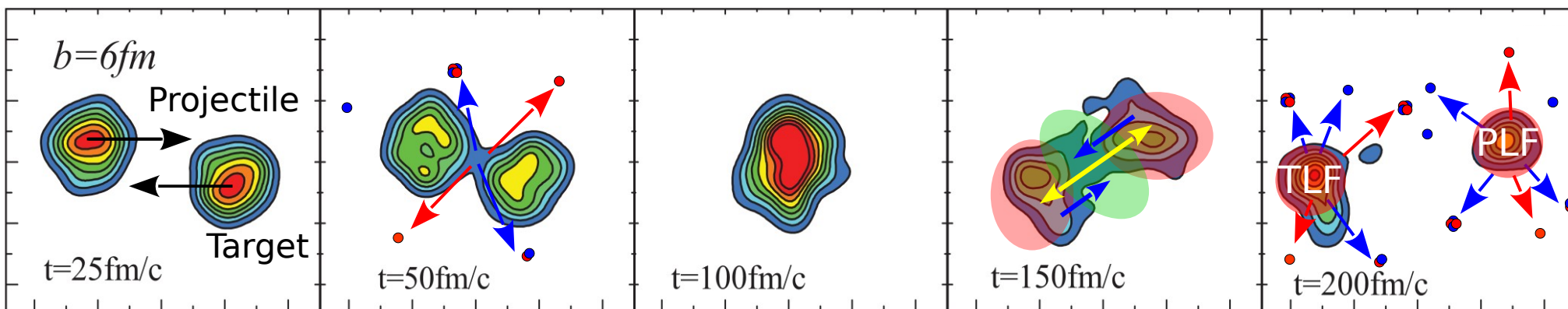
Peripheral collisions

Pre-equilibrium emissions

Mixing

Fragments formation

Statistical decays





Heavy Ion Collisions

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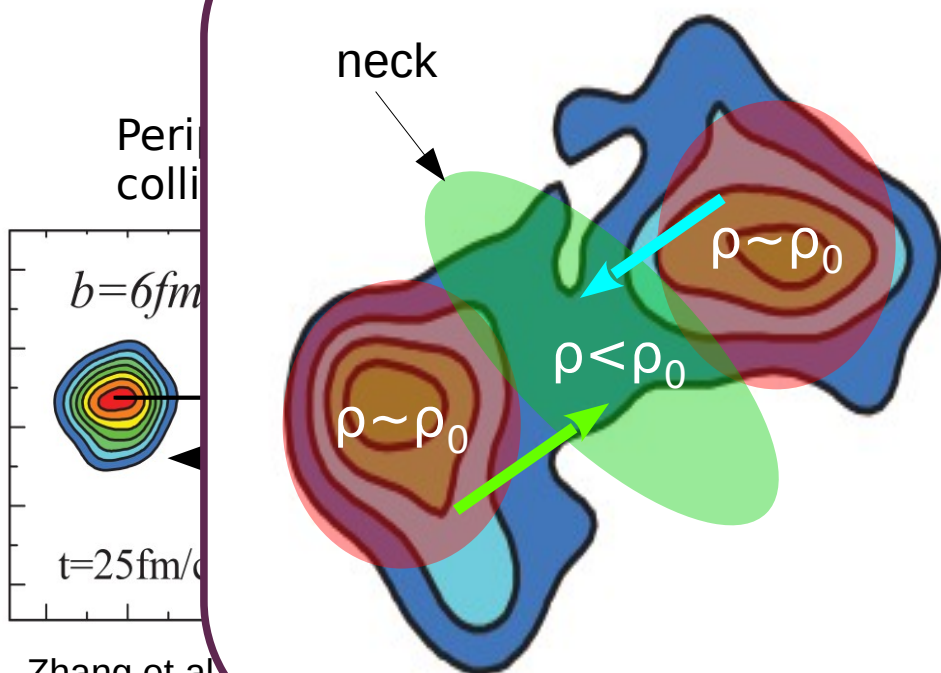
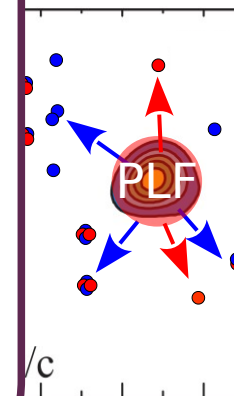
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Isospin migration

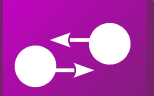
- ρ gradient
- Neutron-enrichment of the neck
- Related to $\frac{\partial \epsilon_{sym}(\rho)}{\partial \rho}$

Particle decays



Zhang et al.

V. Baran et al., Nuc. Phys. A 730 (2004)



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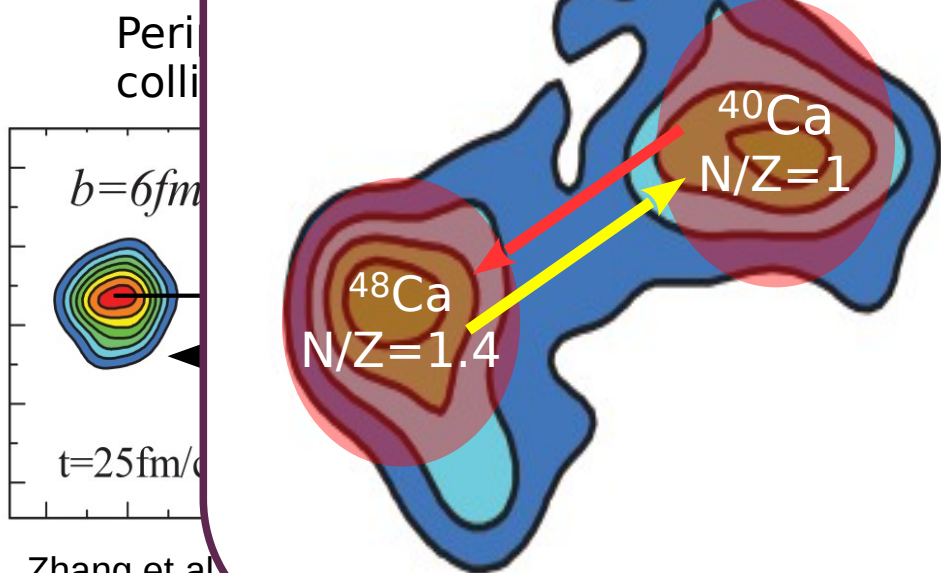
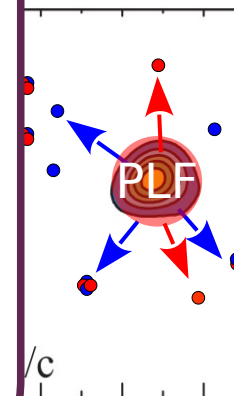
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Isospin diffusion

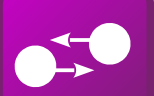
- Minimisation of the **N/Z** concentration gradient
→ neutron/proton currents between proj/targ
- Linked to ϵ_{sym}

Particle decays



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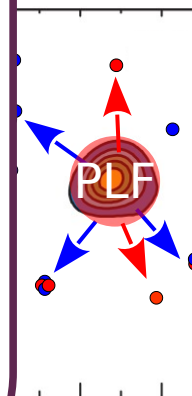
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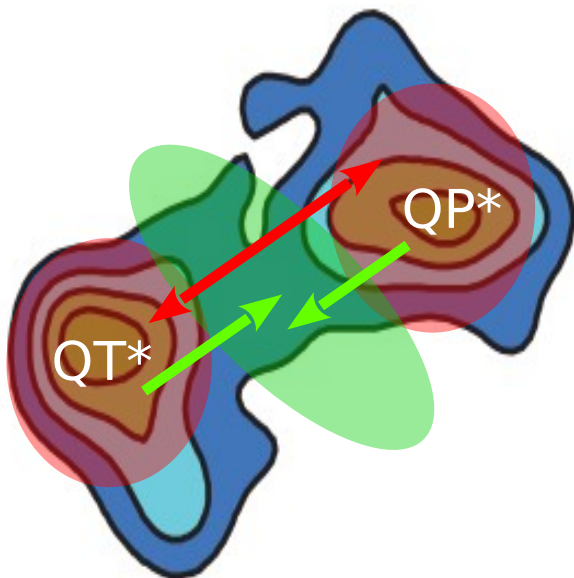
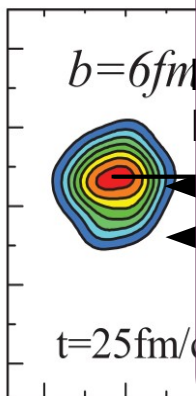
Isospin transport

- Competition between the isospin **migration** and **diffusion**
- Transport phenomena directly linked to ϵ_{sym}
- Depends on the time of interaction between projectile and target
→ beam energy, impact parameter
- Requires :
→ high isotopic resolution
→ special attention to evaporation process
→ evaluation of the interaction and dissipation time

Particle decays



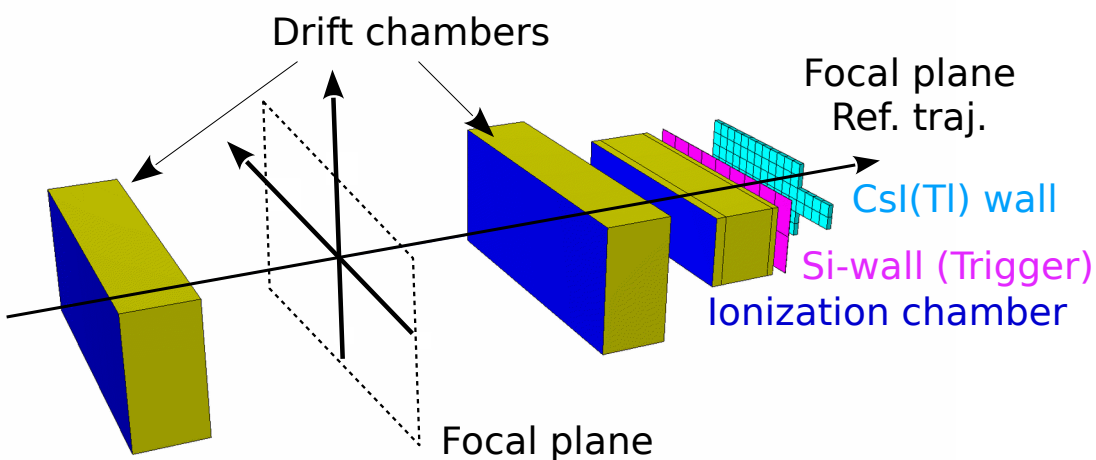
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E503 experiment

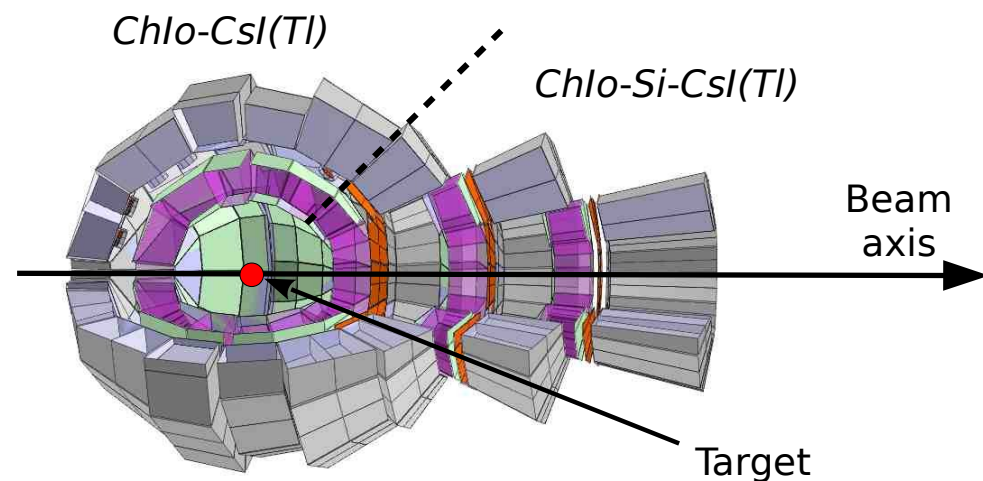
$^{40,48}\text{Ca} + ^{40,48}\text{Ca}$ @ 35 A MeV

VAMOS



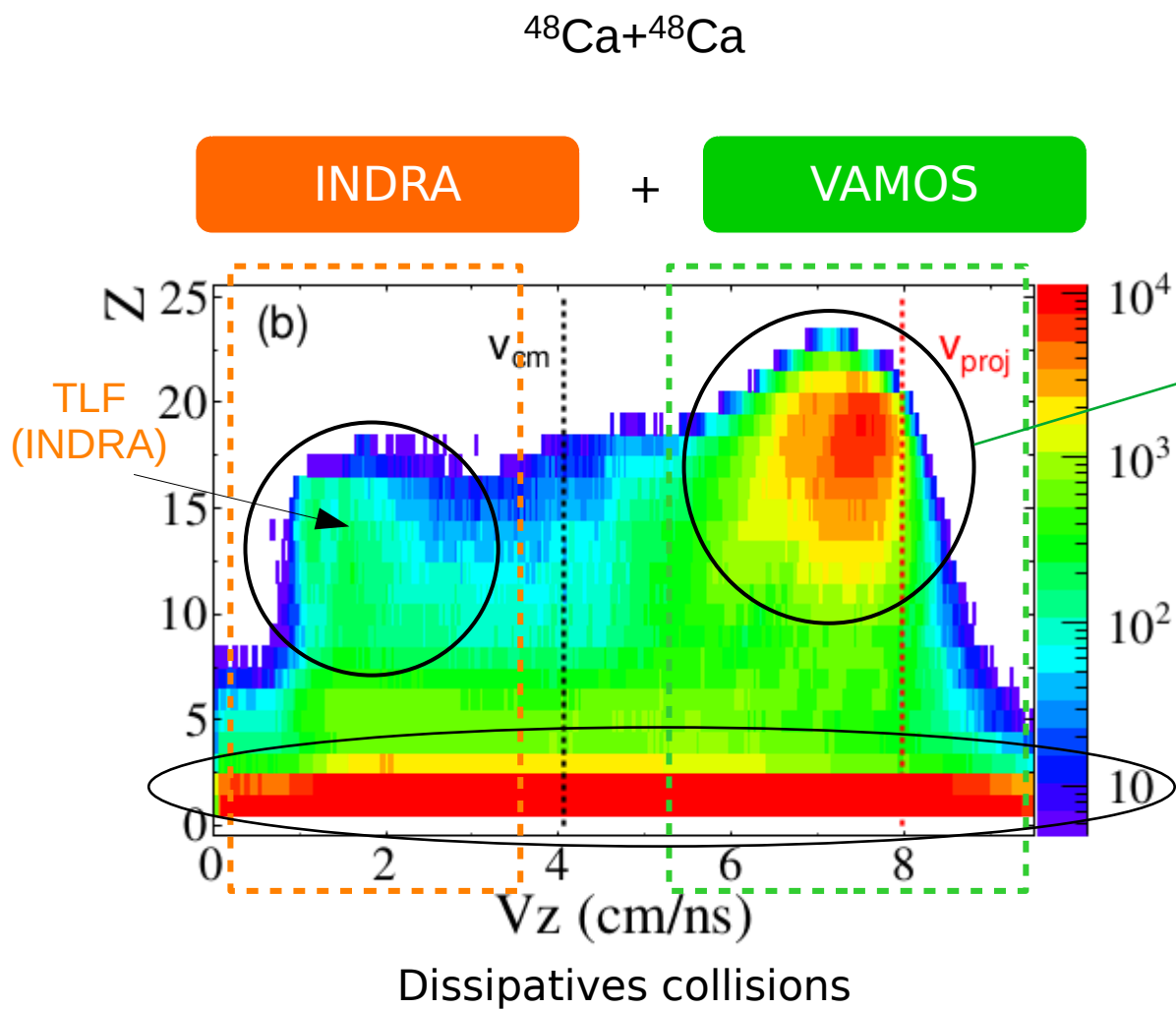
- Si-wall → Acq. Trigger
- Projectile identification (Z,A)
- $\theta_{LAB} \approx 2.5^\circ - 6.5^\circ$
 $\varphi_{LAB} \approx 220^\circ - 320^\circ$
- 12 Bp settings :
→ $B\rho_0 \approx 0.661 - 2.220$ T.m

INDRA

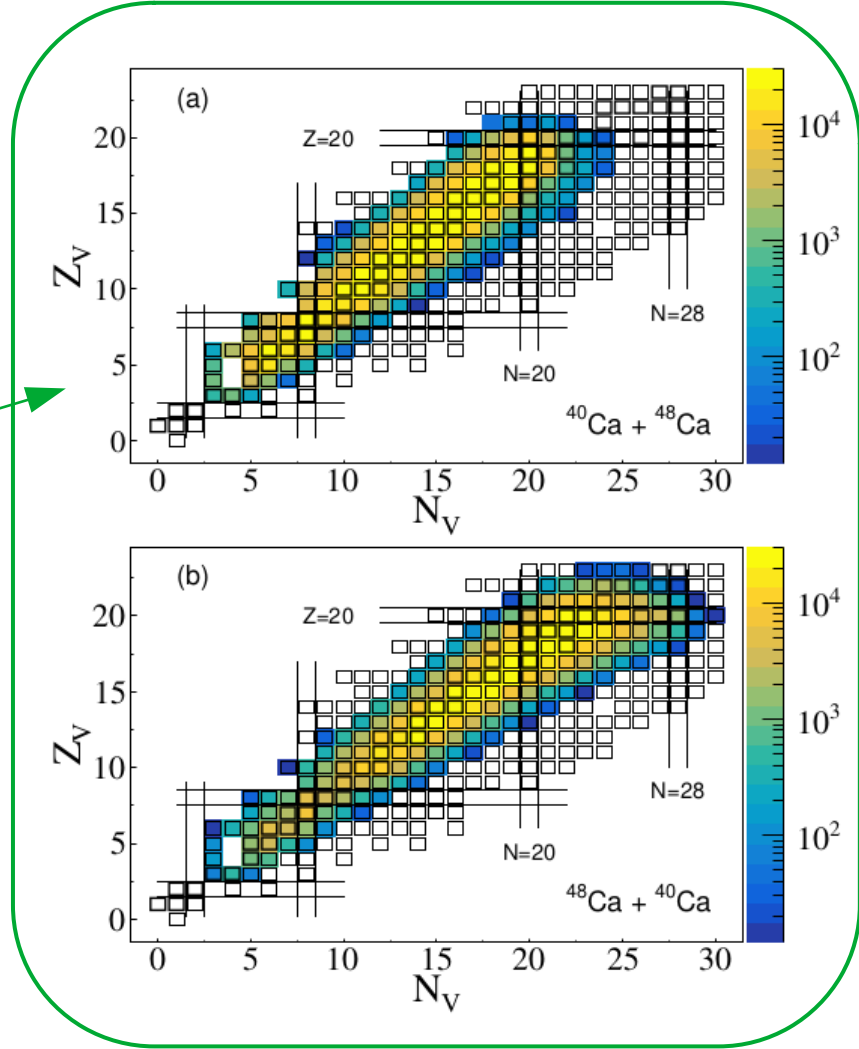


- 14 rings (~300 identification modules)
- Identification
→ (Z,A) for Light Charge Particles ($Z \leq 2$)
→ Z up to $Z \sim 25$
- $\theta_{LAB} \approx 7^\circ - 176^\circ$
- Event characterization (b, E^*, \dots)

General properties of the recorded INDRA-VAMOS events

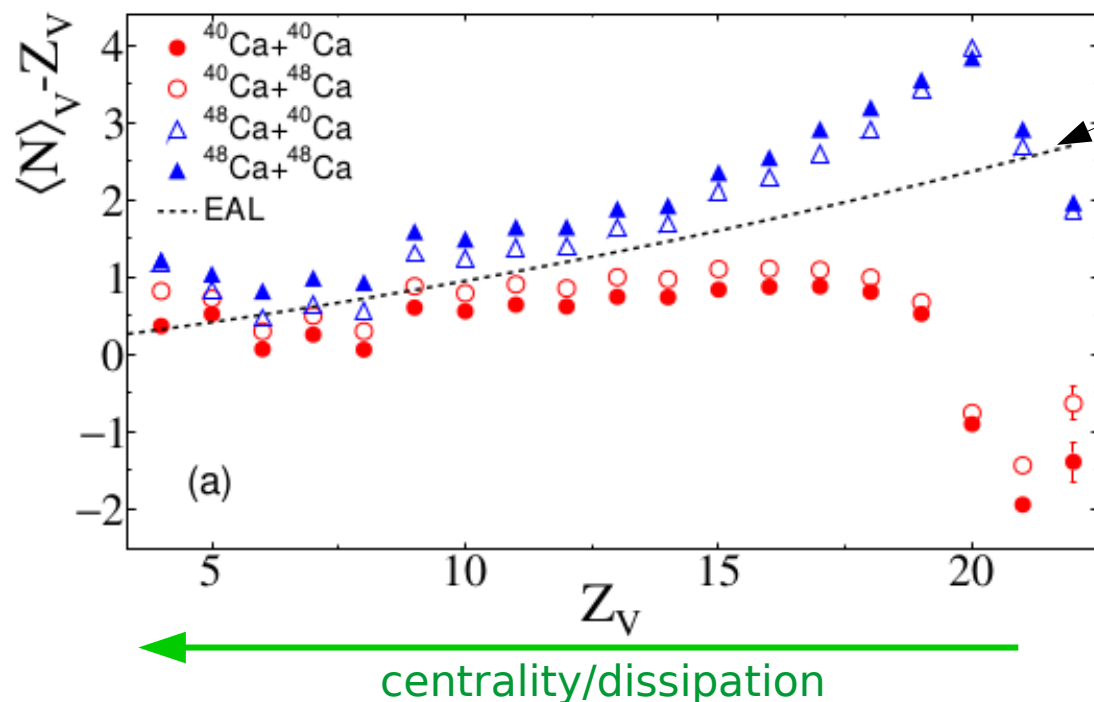


- 3 regions :**
- LCP emissions around v_{CM}
 - PLF and TLF from either side of v_{CM}

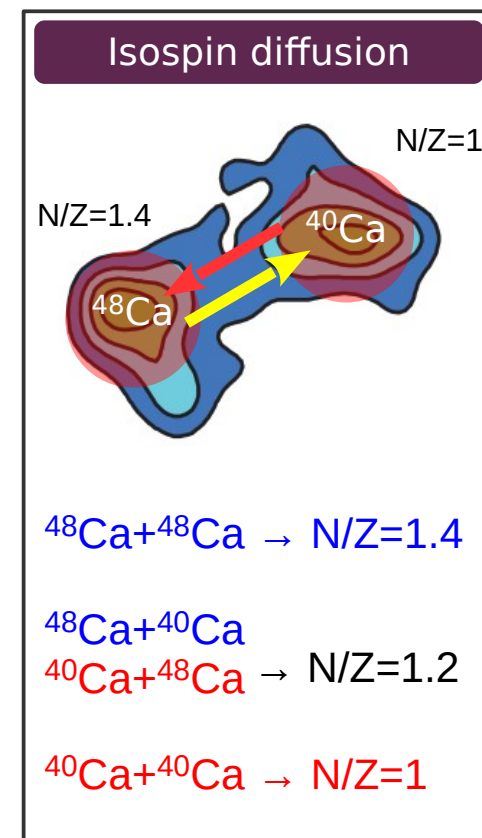


- PLF (Vamos)**
- $V_z \geq 6$ cm/ns
 - $V_z \sim v_{\text{PROJ}}$
 - $Z \sim Z_{\text{PROJ}}$

N-richness of the PLF detected in VAMOS



Evaporative
Attractor
Line

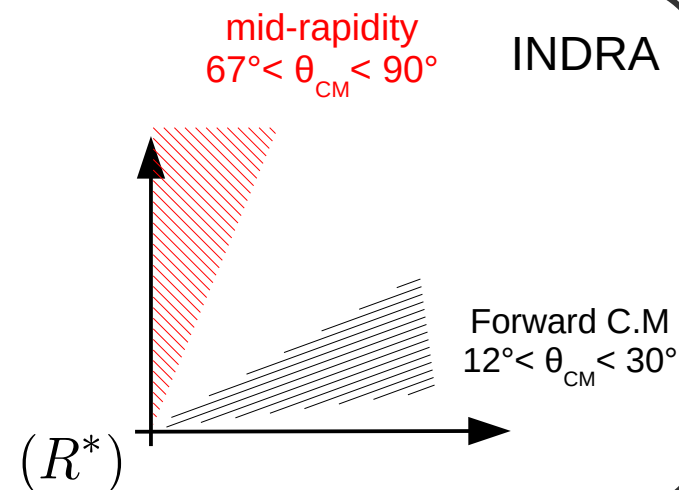


- \neq evolution depending on the system :
 - 1) Projectile
→ number of available neutrons in the entrance channel
 - 2) Target
→ **Isospin diffusion**
- Initial N-Z not reached
→ Statistical decay

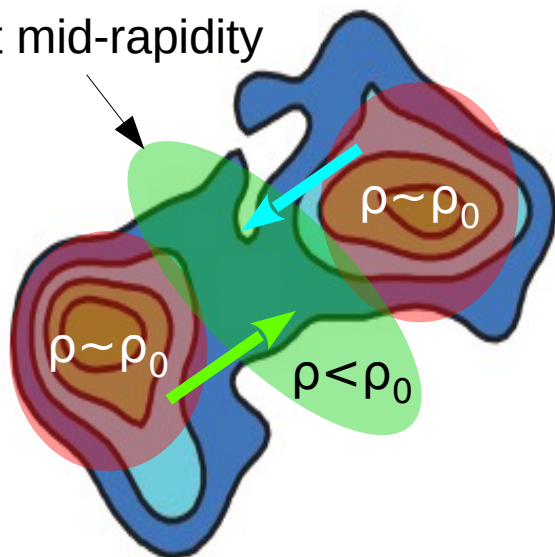
Isotopic ratios

For a given range of Z_ν :

- $(\langle N \rangle / \langle Z \rangle)_{CP} = \frac{\sum_{Nevts} \sum_{\nu} N_{\nu}}{\sum_{Nevts} \sum_{\nu} Z_{\nu}}$
- $\nu = {}^{2,3}H, {}^{3,4,6}He, {}^{6,7,8,9}Li, {}^{7,9,10}Be$
- Neutron-enrichment if $(\langle N \rangle / \langle Z \rangle)_{CP} > 1$



Neck of nuclear matter at mid-rapidity



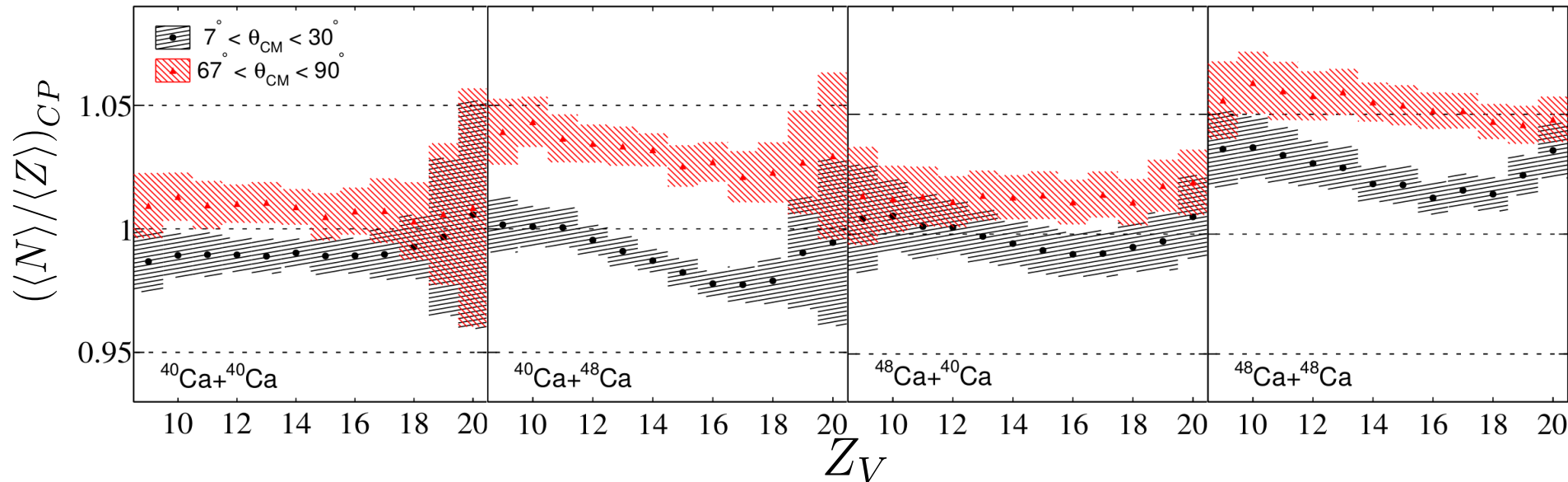
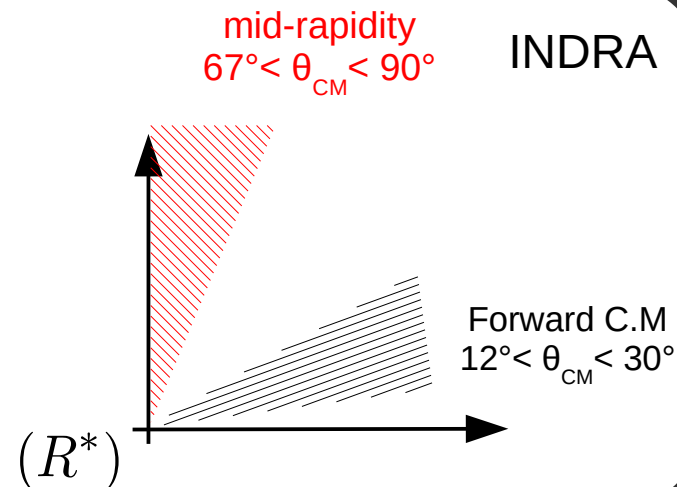
Isospin migration

- ρ gradient
- Mid-rapidity n-enrichment
- Linked to $\frac{\partial \epsilon_{sym}(\rho)}{\partial \rho}$

Isotopic ratios

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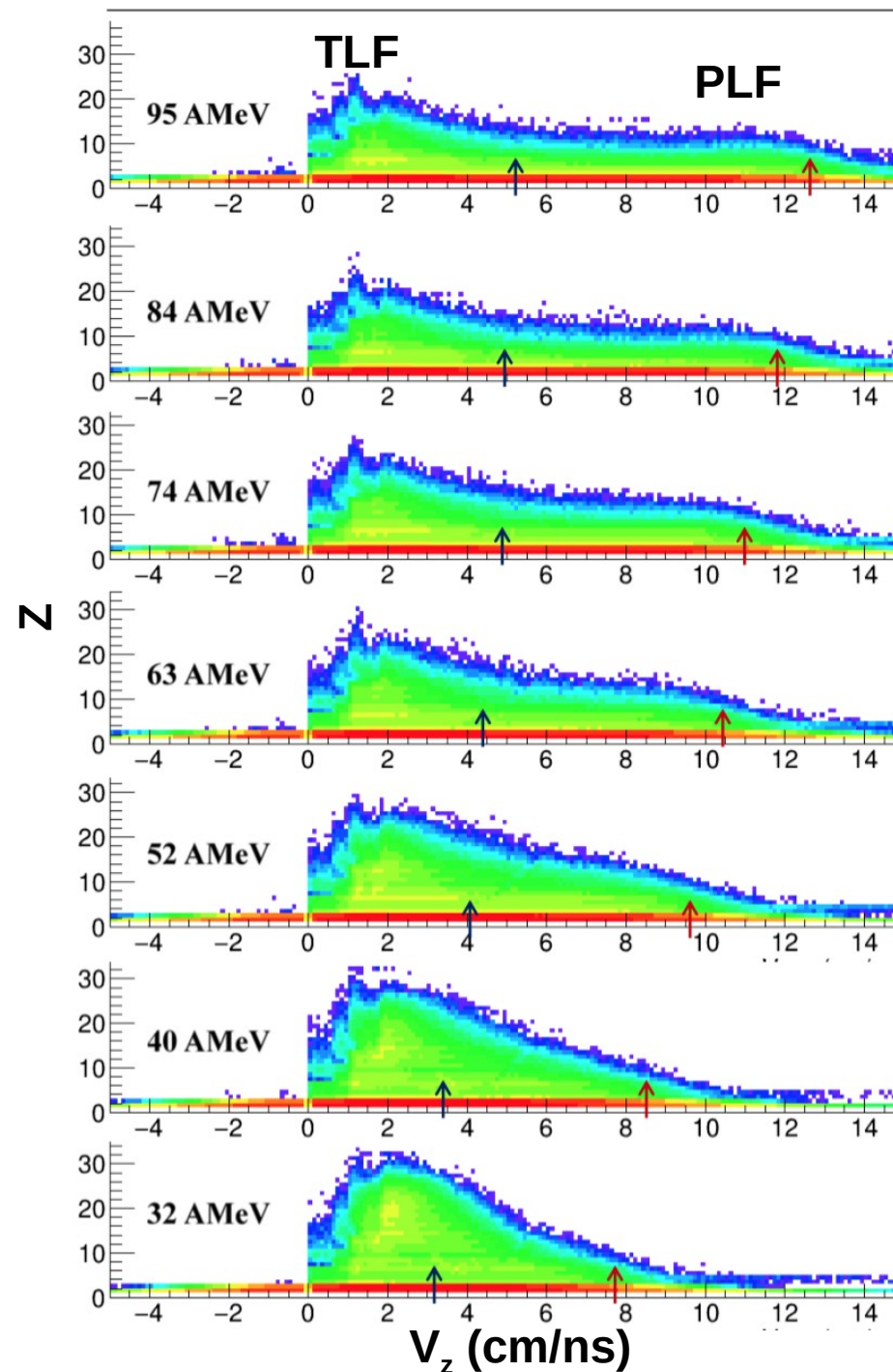


In the case of symmetric systems :

- mid-rapidity neutron-enrichment
- direct experimental measure of the **isospin migration**

Head-on collisions

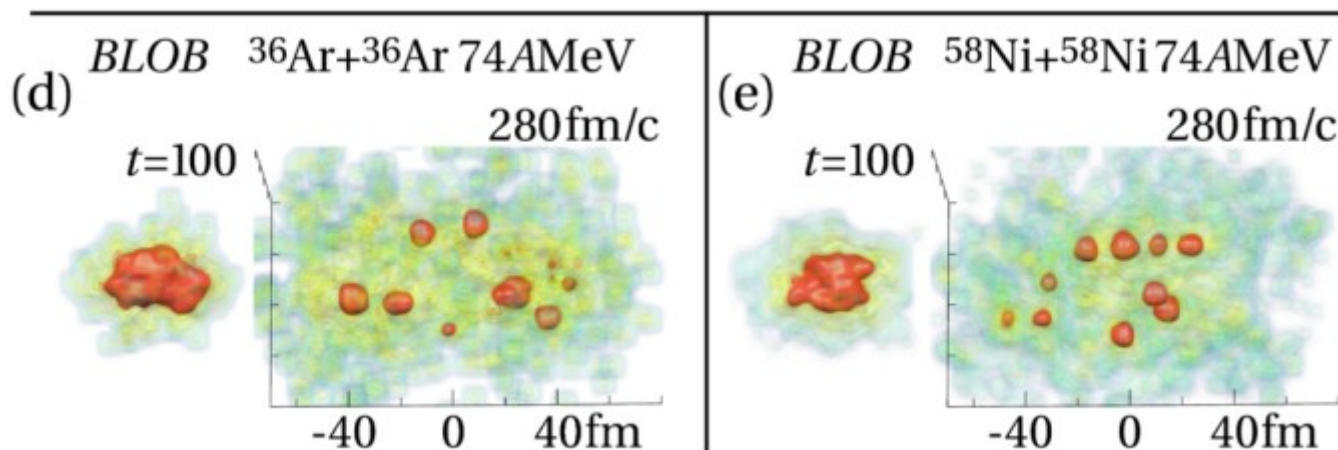
- When the impact parameter decreases and the beam energy increases, the fragmentation may become more complicated than the former case...
- Illustration from $^{36}\text{Ar}+^{58}\text{Ni}$ **central collisions** @ 32, 40, 52, 63, 74, 84 and 95 AMeV
- Observed topology different from multifragmentation and vaporisation :
 - Break-up asymmetry in forward vs backward CM
 - Granular projectile fragmentation topology



Jet fragmentation in BLOB

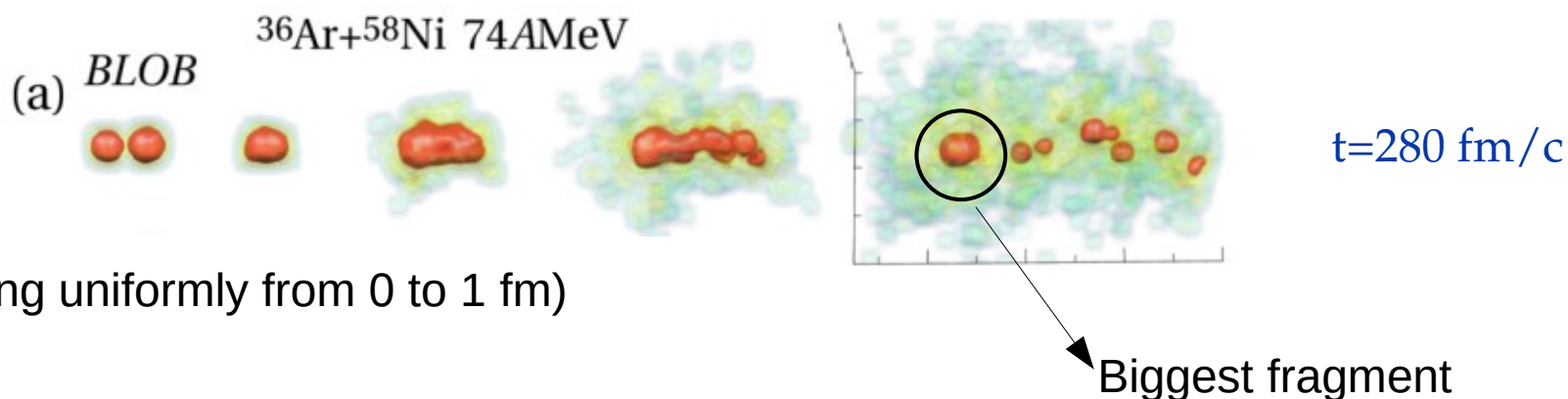
- Boltzmann-Langevin One-Body :
 - Stochastic transport theory (3D)
 - Mean-field description
 - n-n collisions
 - Langevin-type fluctuations
- Symmetric ($^{36}\text{Ar}+^{36}\text{Ar}$ or $^{58}\text{Ni}+^{58}\text{Ni}$) :
 - significant radial expansion
 - signature of multifragmentation and vaporization mechanisms

$^{36}\text{Ar}+^{36}\text{Ar}$ and $^{58}\text{Ni}+^{58}\text{Ni}$ @ 74 AMeV with BLOB
(b varying uniformly from 0 to 1 fm)



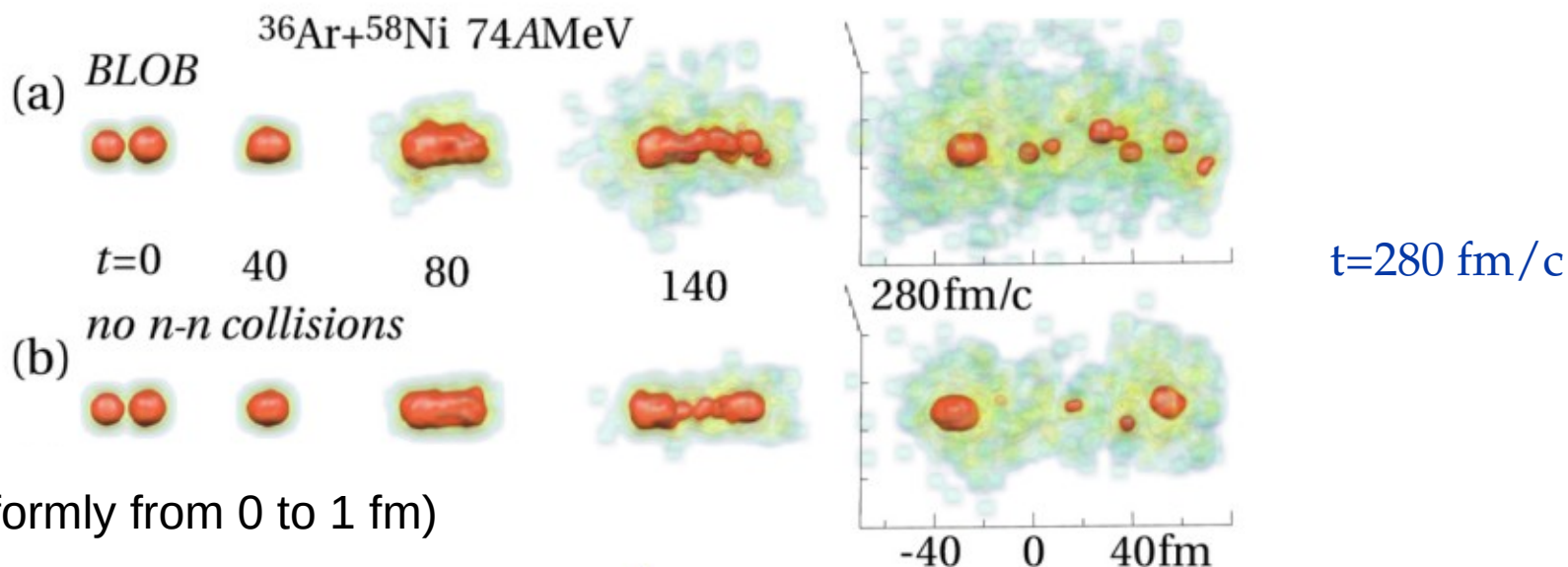
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 - columnar jet formation in the forward sector relative to the biggest fragment
 - since early time this jet experiences a density drop along longitudinal axis



Jet fragmentation in BLOB

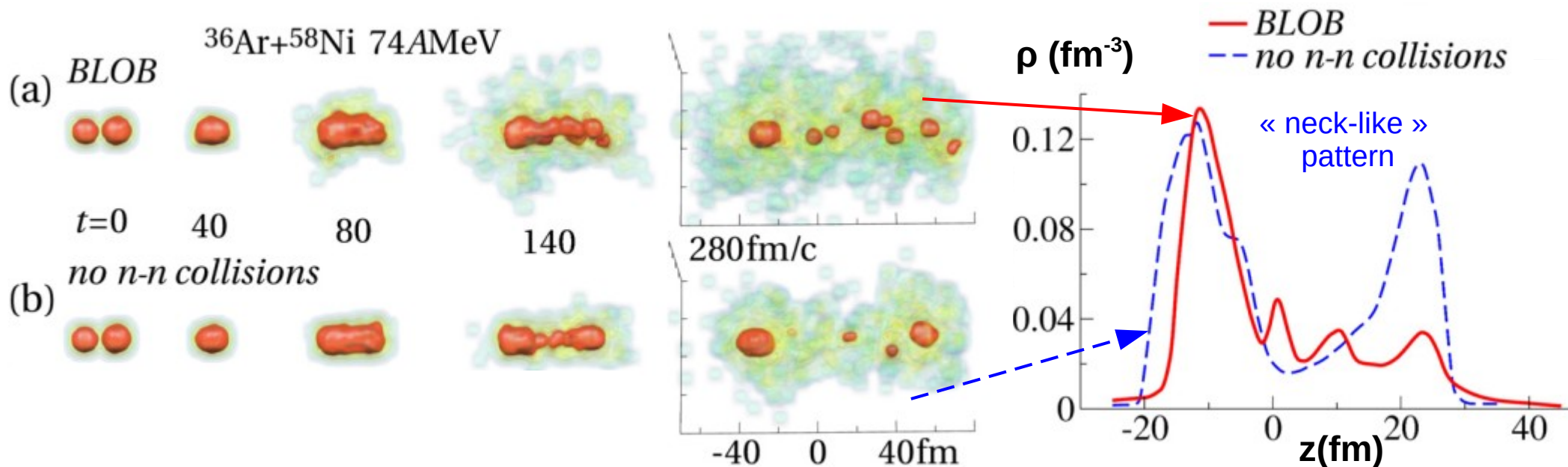
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 - a collisionless approach leads to a neck-like pattern instead



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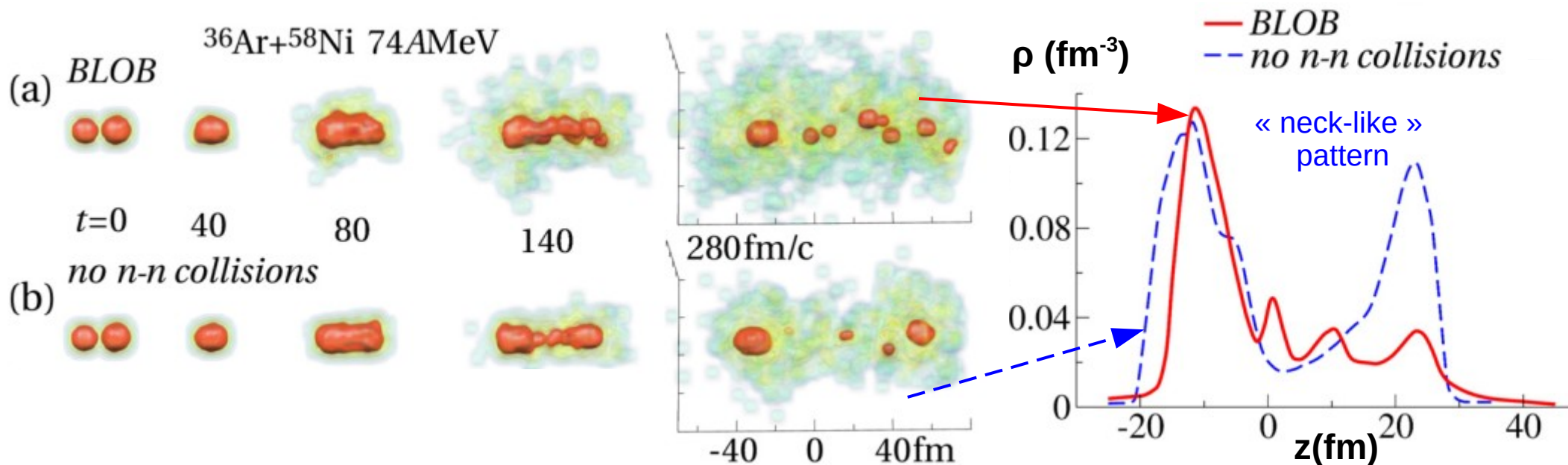


Jet fragmentation in BLOB

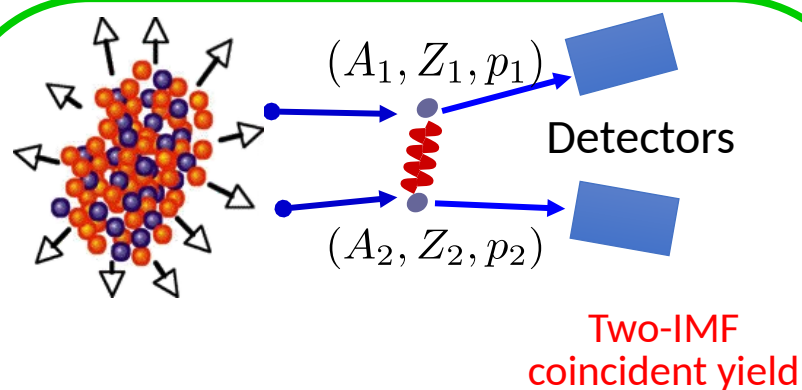
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→ **Projectile region = prediction intense volume-like fast break-up ;**
 → **Target region = long time-scale surface-like emissions (evaporative).**



- Femtoscscopy :
 - Term used for estimating distances, lifetimes and densities on the femtoscopic scale.
- IMF-IMF ($Z > 2$) correlation functions :
 - Interferometry studies ;
 - Allows to probe space-time properties of the collision products ;
 - The shape of the correlation function is strongly affected by fragment emission time at small relative velocities (Coulomb anti-correlation).



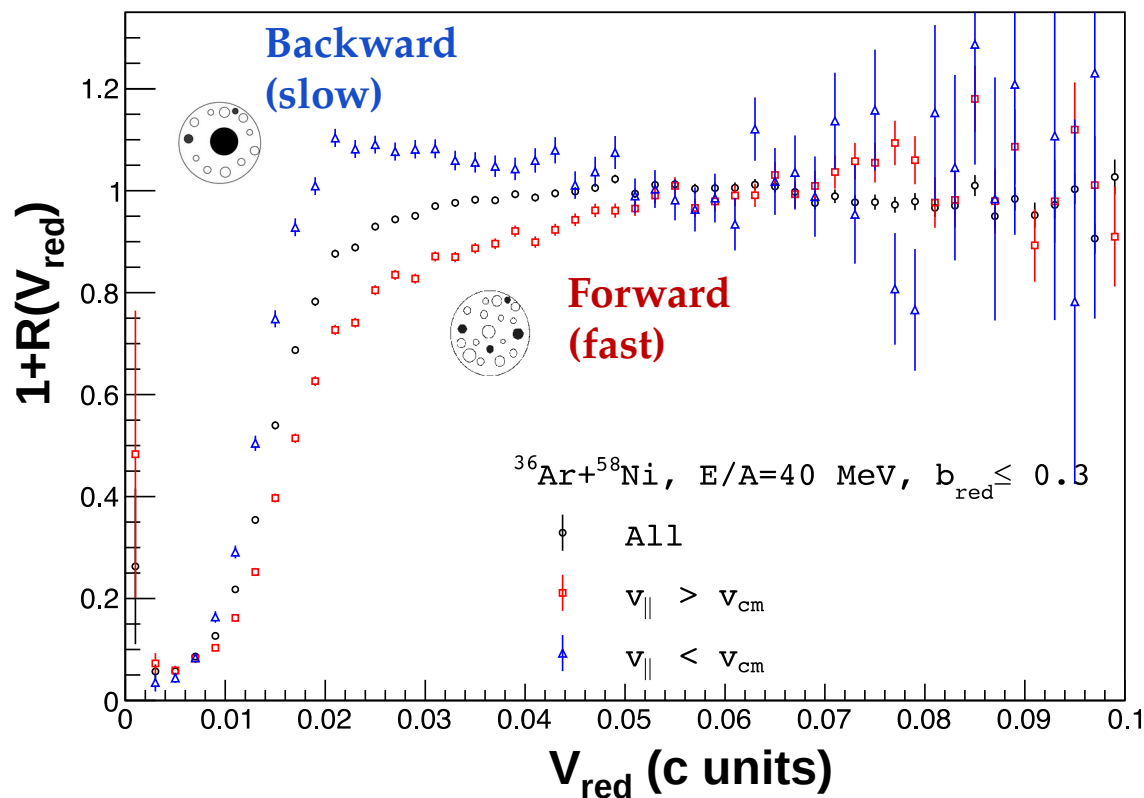
$$1 + R(V_{red}) = C \cdot \frac{\sum Y_{coinc}(p_1, p_2)}{\sum Y_{unco}(p_1, p_2)}$$

Approximation of the yields of two uncorrelated IMF (event mixing)

$$V_{red} = V_{rel} / \sqrt{Z_1 + Z_2}$$

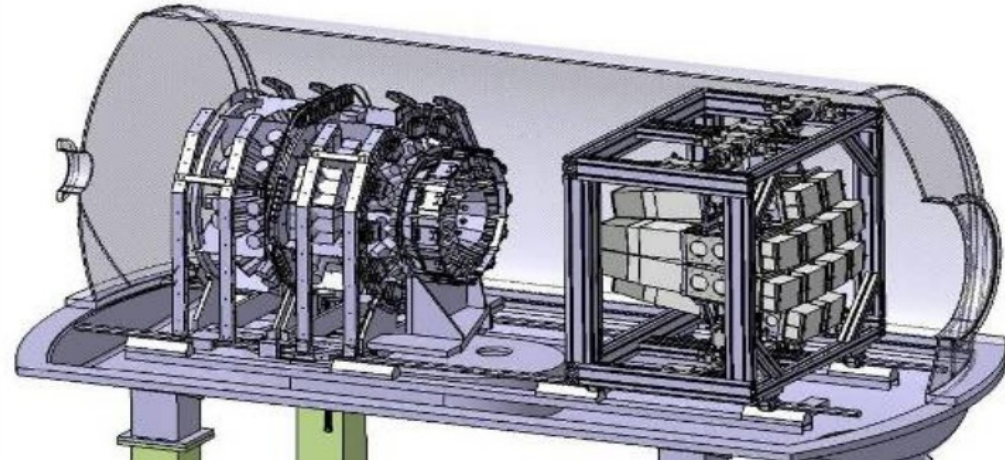
G. Verde, EPJA 30 (2006)

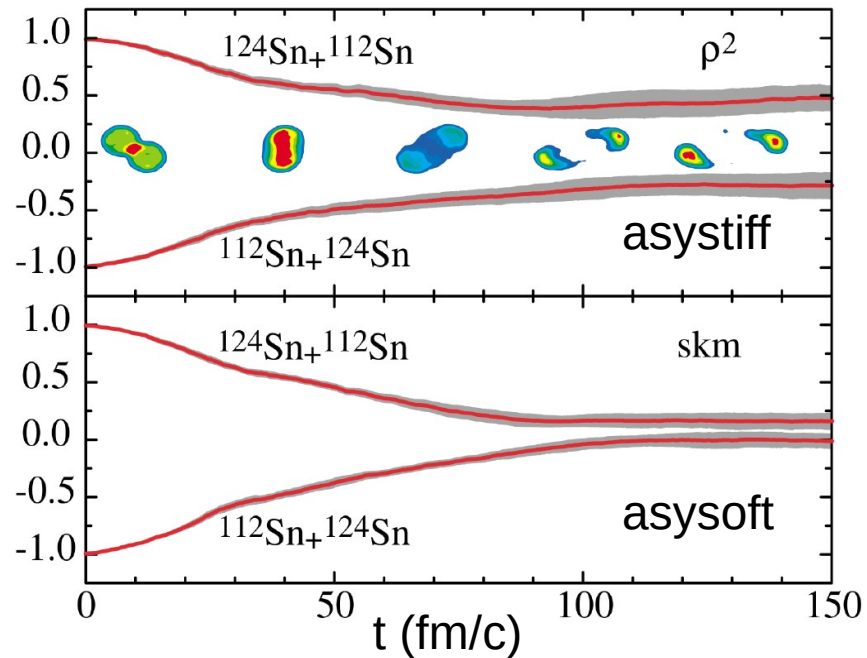
$^{36}\text{Ar} + ^{58}\text{Ni}$ @ 40 A MeV with INDRA



- INDRA-VAMOS experiment allowed to probe the isospin transport phenomena, predicted by transport models, with $^{40,48}\text{Ca}+^{40,48}\text{Ca}$ peripheral collisions
 - experimental evidence of isospin diffusion and migration ;
 - due to the use of VAMOS and the trigger conditions, complementary results can be accessed with INDRA-FAZIA.
- For more central collisions :
 - $^{36}\text{Ar}+^{58}\text{Ni}$ asymmetric collisions measured with INDRA show a particular topology that has not been explicitly addressed so far ;
 - BLOB dynamical simulations evidenced the appearance of nuclear jets formation in the forward direction ;
 - These collimated streams of clusters are expected to be at low-density ;
 - Interplay of surface and volume instabilities.
- These predictions point to new detection systems measuring on a event-by-event basis :
 - isotopic identification ;
 - angular correlations ;
 - cluster coincidences.

- Isospin transport :
 - INDRA-VAMOS drawbacks (normalization, trigger condition)
 - Effect of beam energy (density) ?
 - Impact parameter estimation ?
 - Complementary results with INDRA-FAZIA (see Caterina Ciampi talk)
- Correlation function :
 - Improved angular resolution with FAZIA ;
 - Fix and establish procedures for the study of correlation functions (event mixing, effect of global observables and conservation laws) using existing INDRA data;
 - Extension to INDRA-FAZIA
- Extensive comparisons with different models to link the observations to transport properties :
 - BLOB
 - QMD
 - AMD (see Catalin Frosin talk) ...





$$R_i^x = \frac{2(x^M - x^{eq})}{(x^H - x^L)}$$

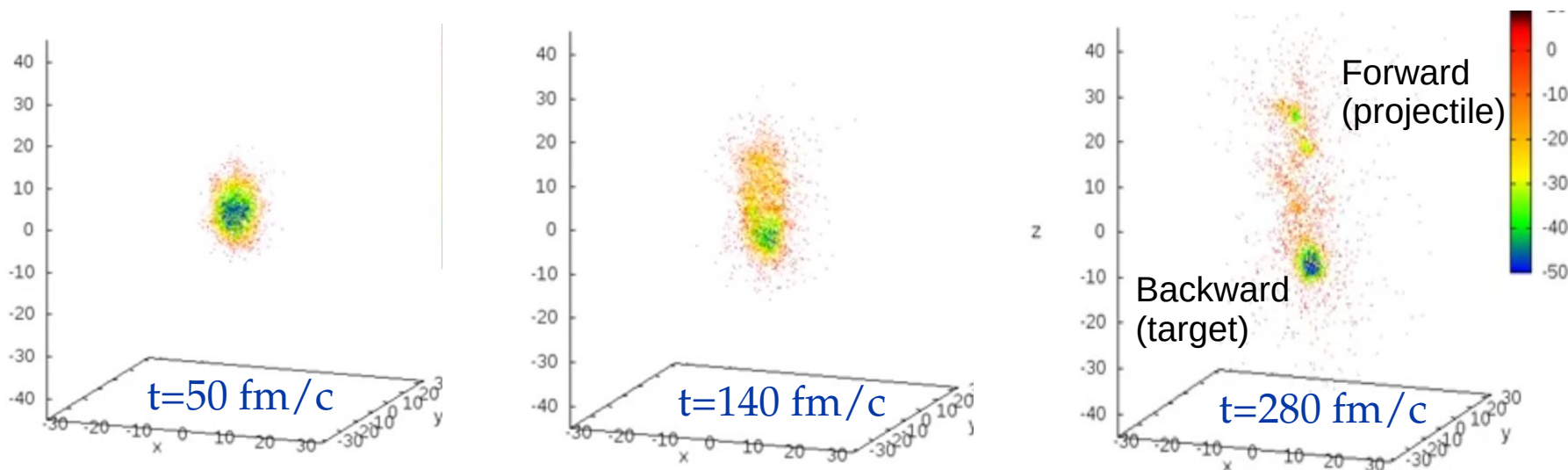
$$x^{eq} = \frac{x^H + x^L}{2}$$

- x = observable sensitive to isospin transport
- $x = \pm 1$ → no diffusion
- $x = 0$ → diffusion with complete equilibrium

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 - significant radial expansion
 - signature of multifragmentation and vaporization mechanisms
- $^{36}\text{Ar}+^{58}\text{Ni}$:
 - jet formation of fast-streaming low-density matter
 - this density drop also triggers isospin effects

$^{36}\text{Ar}+^{58}\text{Ni}$ @ 40 AMeV with BLOB



Taylor-Young dev around $\delta=0$:

$$\epsilon(\rho, \delta) = \epsilon(\rho, \delta=0) + \epsilon_{sym}(\rho) \cdot \delta^2 + \dots \quad \epsilon_{sym} = \frac{1}{2} \frac{\partial^2 \epsilon(\rho, \delta)}{\partial \delta^2} \Big|_{\delta=0}$$

Ex. of parametrization :

$$\epsilon_{sym}(\rho) = \frac{C_{kin}}{2} \left(\frac{\rho}{\rho_0} \right)^{2/3} + \frac{C_{pot}}{2} \left(\frac{\rho}{\rho_0} \right)^y$$

Fermi gaz N-N interaction

Ex : Second-order limited dev. around ρ_0 :

$$\epsilon_{sym}(\rho) = S_0 + \frac{L}{3} \left(\frac{\rho - \rho_0}{\rho_0} \right) + \frac{K_{sym}}{18} \left(\frac{\rho - \rho_0}{\rho_0} \right)^2 + \mathcal{O} \left\{ \left(\frac{\rho - \rho_0}{\rho_0} \right) \right\}^3$$

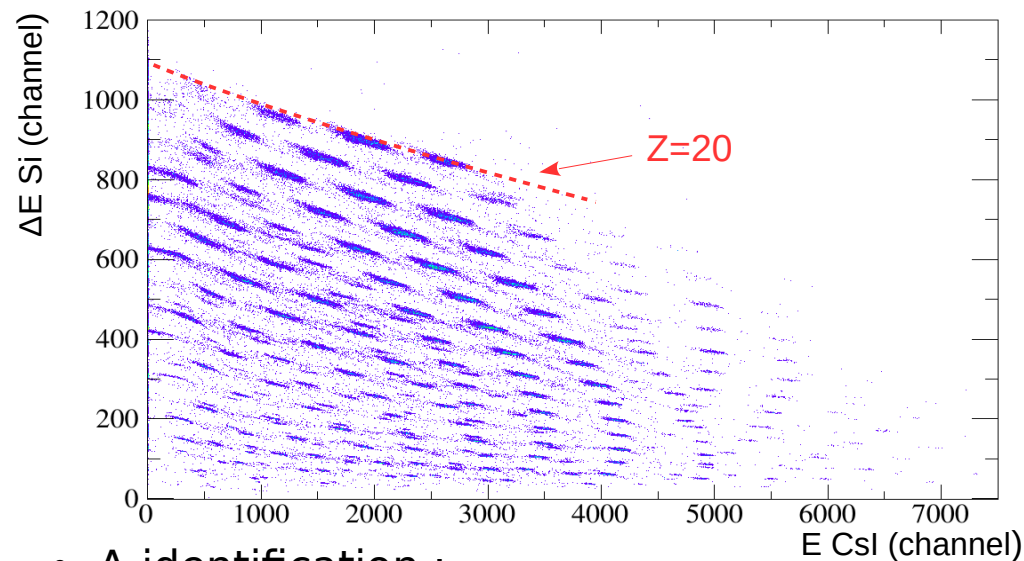
$$L = 3\rho_0 \frac{\partial \epsilon_{sym}(\rho)}{\partial \rho} \Big|_{\rho=\rho_0} \quad K_{sym} = 9\rho_0^2 \frac{\partial^2 \epsilon_{sym}(\rho)}{\partial^2 \rho} \Big|_{\rho=\rho_0}$$

« Slope » param.
« Incompressibility » param.

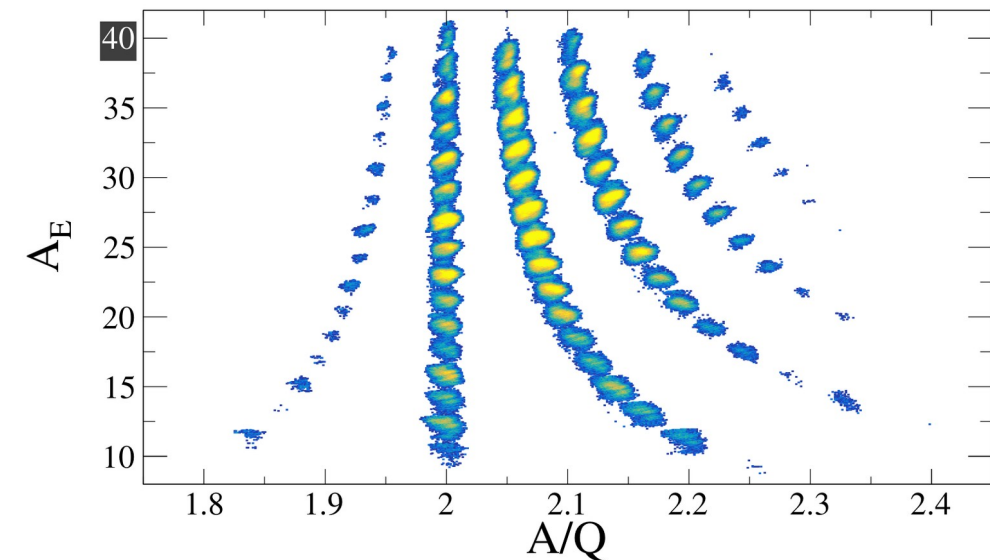
Particle ID

VAMOS

- ΔE -E \rightarrow Z-identification:

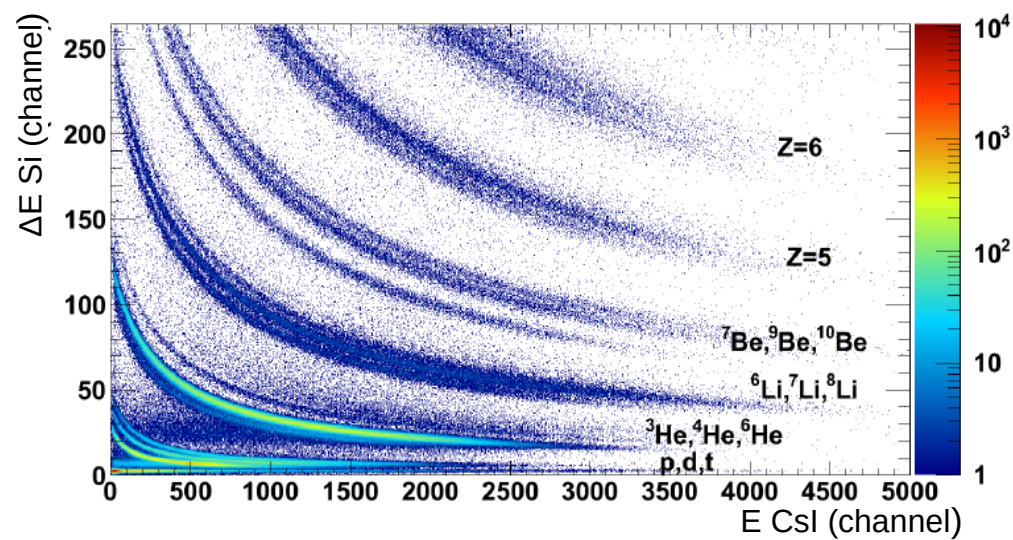


- A-identification :

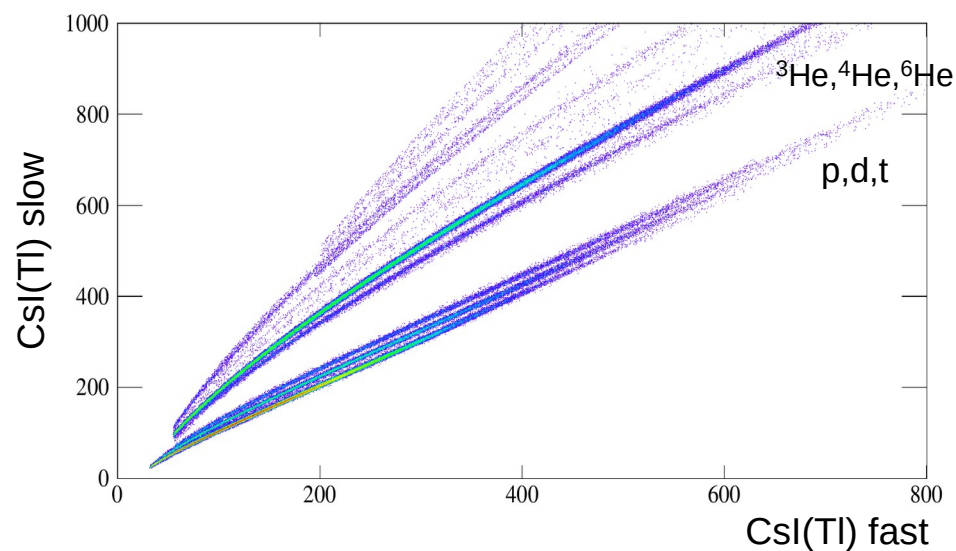


INDRA

- ΔE -E \rightarrow Z-identification :



- Pulse-shape (slow/fast) CsI(Tl) :

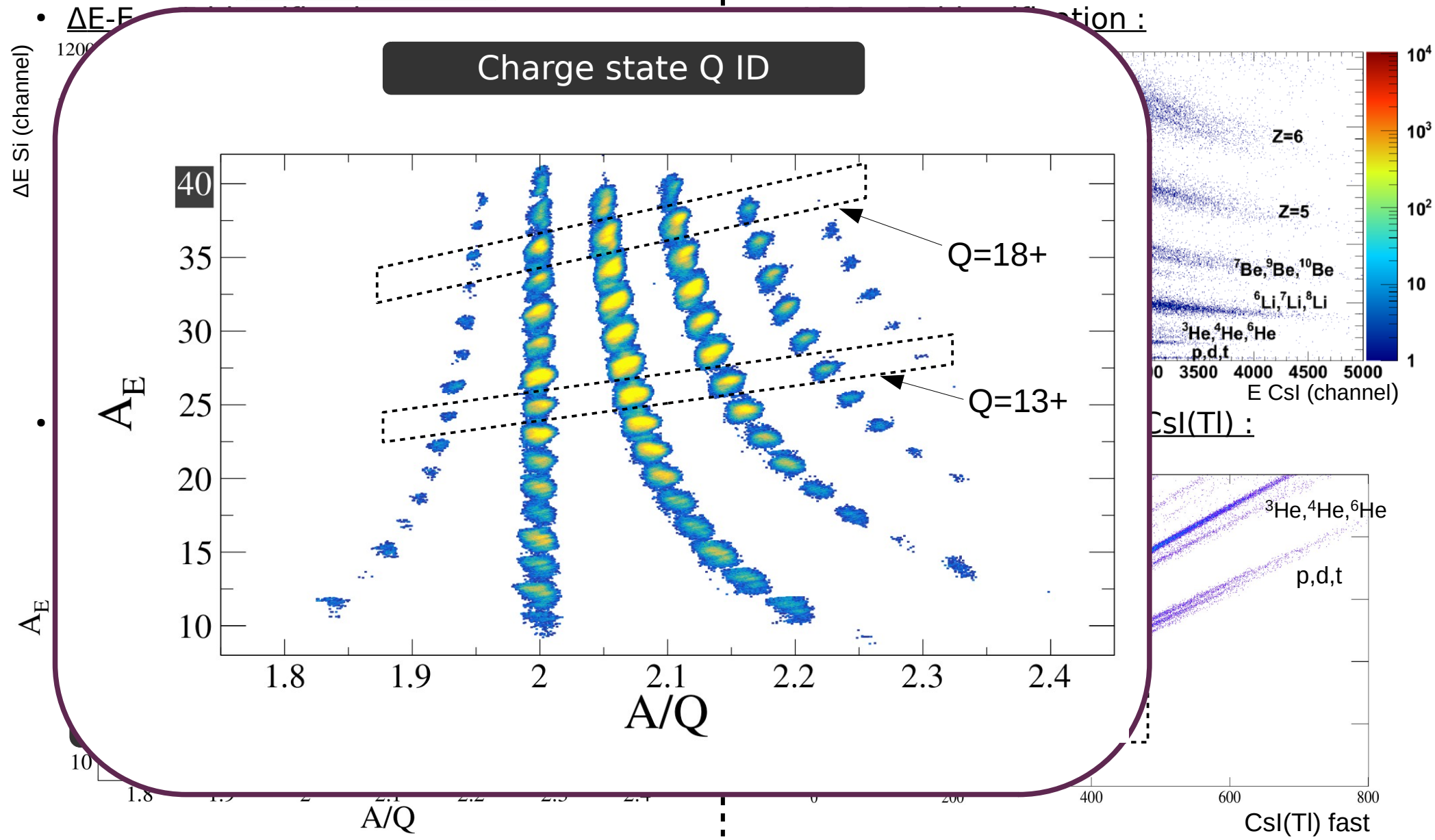


Particle ID

VAMOS

INDRA

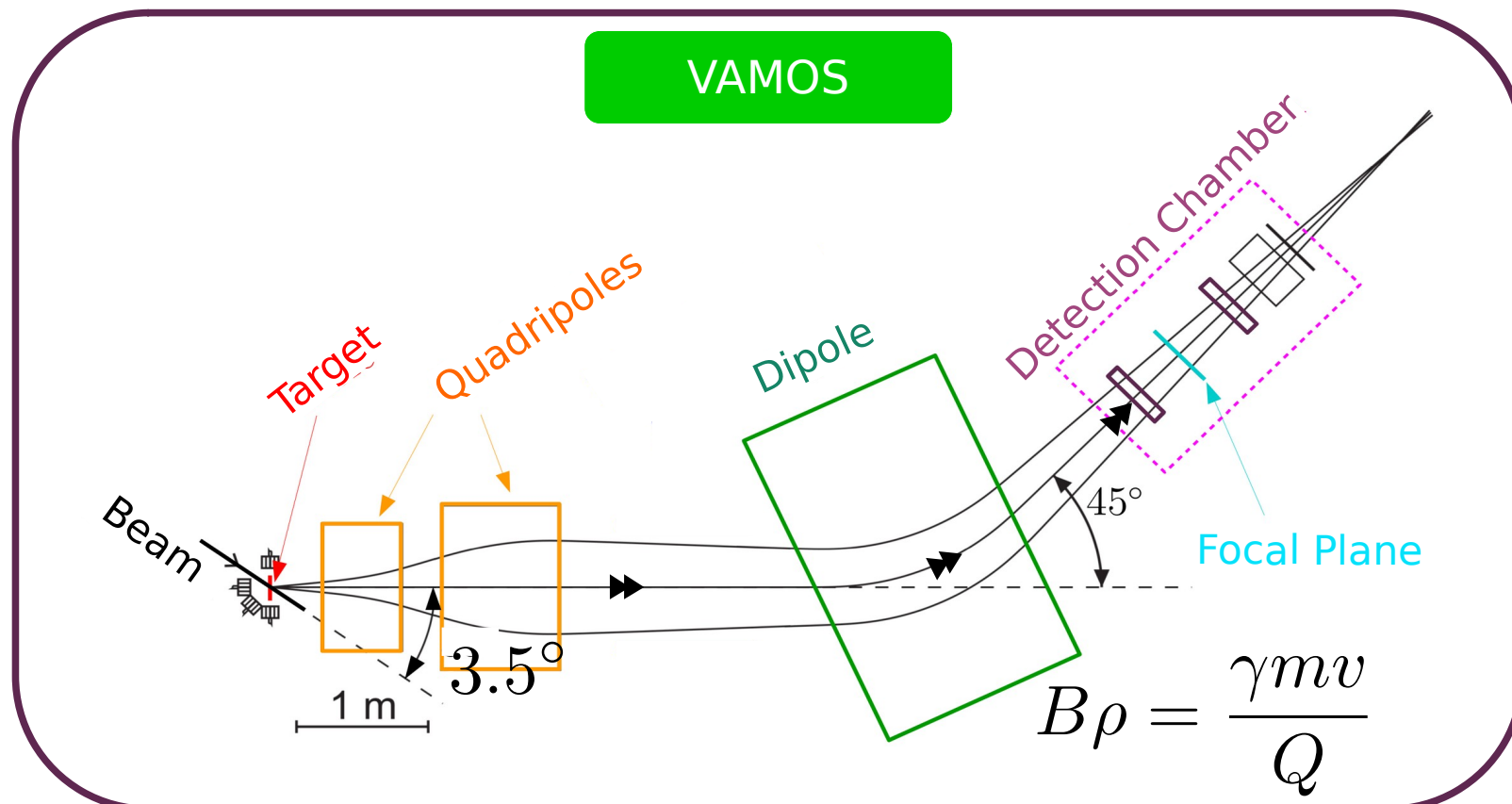
Charge state Q ID



E503 experiment

$40,48\text{Ca} + 40,48\text{Ca}$ @ 35 A MeV

- [1] S. Pullanhiotan et al., NIM A 593
- [2] H. Savajols et. al, Nuc. Phy. A 746
- [3] M. Rejmund et al., NIM A 646

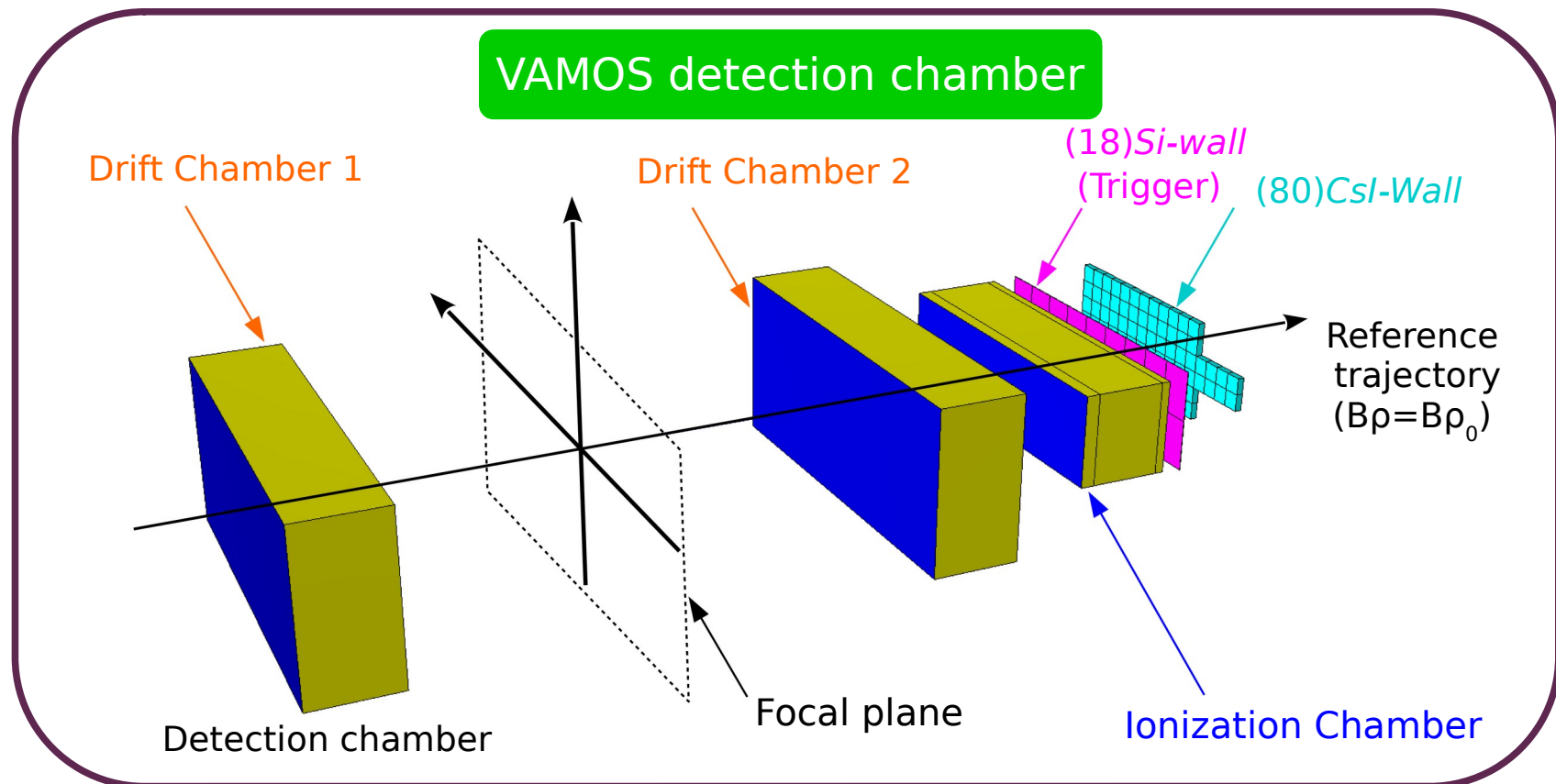


E503 experiment

$^{40,48}\text{Ca} + ^{40,48}\text{Ca}$ @ 35 A MeV

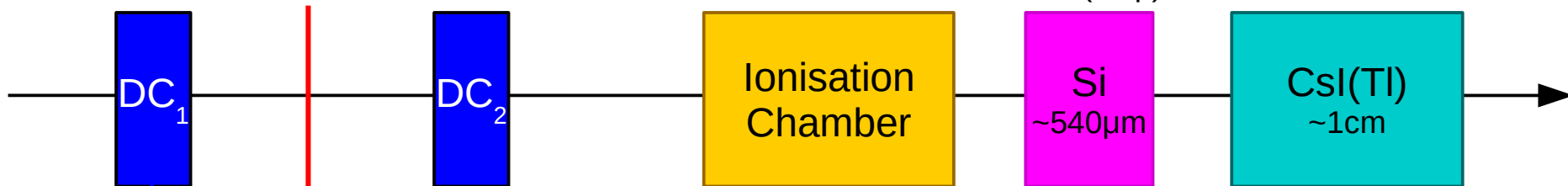
- [1] S. Pullanhiotan et al., NIM A 593
- [2] H. Savajols et. al, Nuc. Phy. A 746
- [3] M. Rejmund et al., NIM A 646

« Software spectrometer » : trajectory reconstruction from focal plane to the target point using simulations



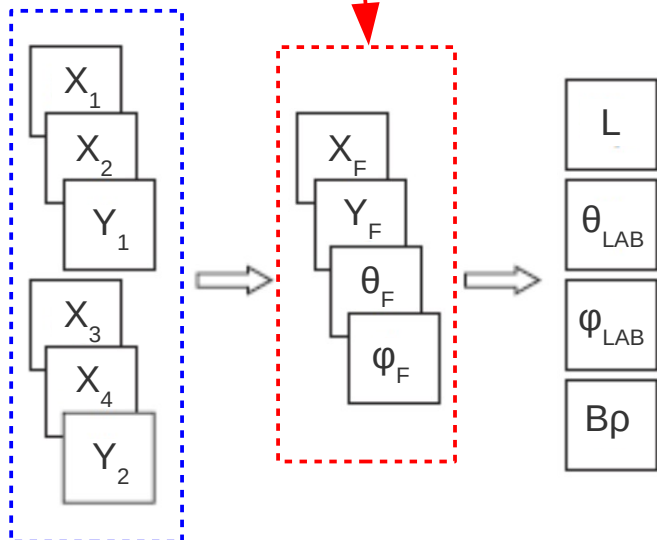
Particle ID with VAMOS

Drift Chambers



1

Focal Plan



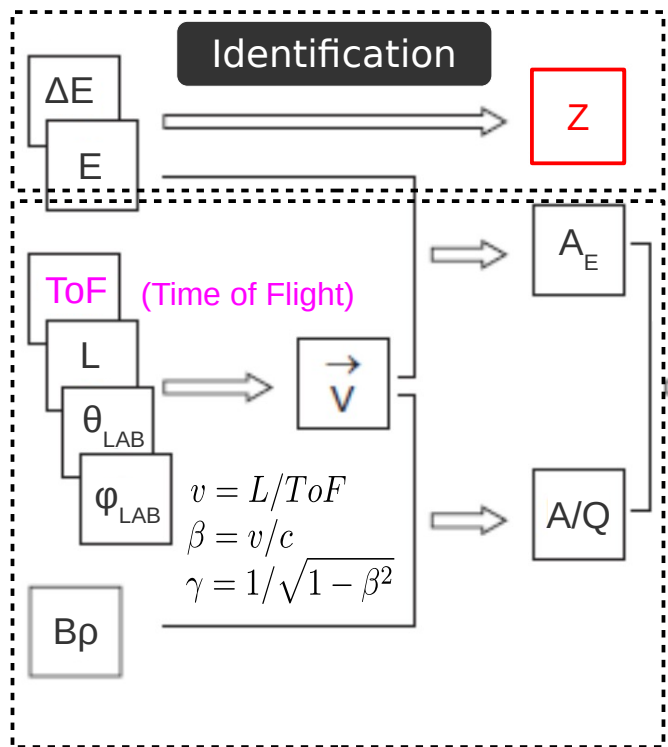
Reconstruction at focal plan

→ Drift chambers

Reconstruction at target point

→ Simulations (ZGOUBI)

2



ToF : start = HF signal HF (cyclotron)
stop = Si signal

$$A_E = \frac{E_{TOT}}{m_0(\gamma - 1)}$$

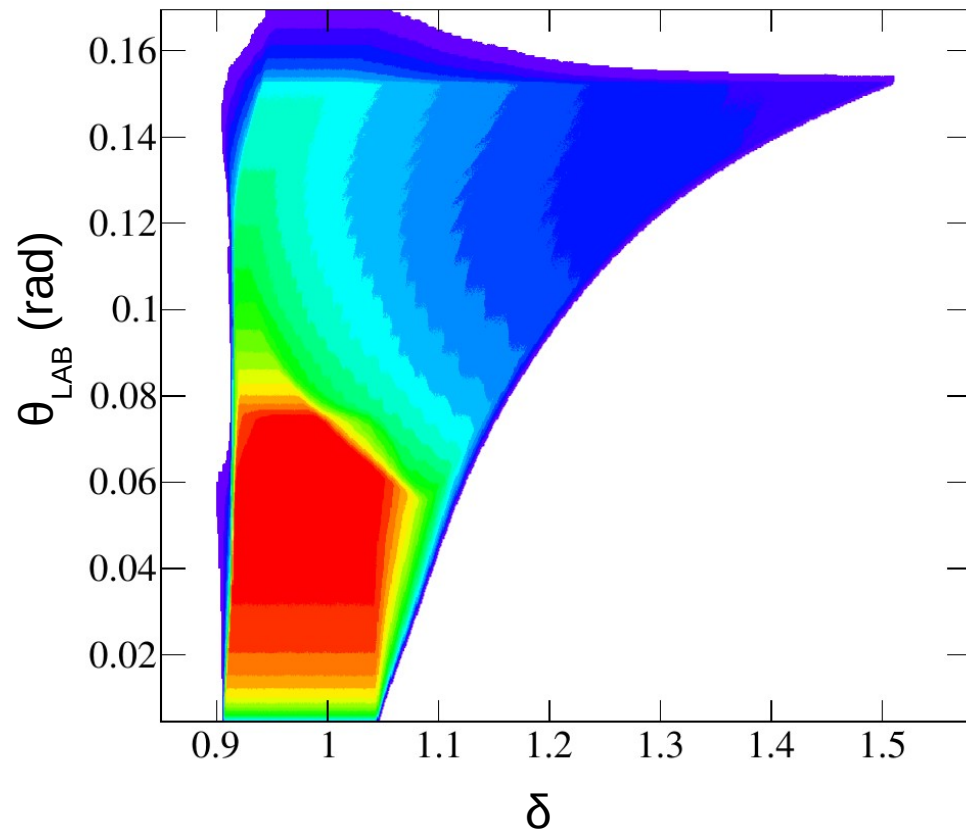
$$\frac{A}{Q} = \frac{B\rho}{3.107\beta}$$

How to normalize the events ?

- Beam intensity corrections $\rightarrow I_{beam}$
- Dead Time corrections $\rightarrow DT$

- Magnetic rigidity overlaps $\rightarrow \delta$
- VAMOS acceptance corrections :

VAMOS geometrical efficiency



$$\rightarrow \epsilon_{geo}(\delta, \theta_{LAB}) = \frac{\Delta^2 \Omega(\delta, \theta_{LAB})}{4\pi}$$

efficacité géométrique

angle solide effectif

$$\delta = B\rho / B\rho_0$$

\rightarrow Simulation of more than 10^6 trajectoires with Zgoubi to estimate $\epsilon_{geo}(\delta, \theta_{LAB})$

A weight $W(I_{beam}, DT, \delta, \theta_{LAB})$ is applied event-by-event